Development and Control of a condensation system using Peltier Cells

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Thesis to obtain the Master of Science Degree in Electrical and Computer Engineering

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April 2014
To...
I would like to thank…
Abstract

This work proposes the development and control of a condensation system using Peltier cells. The condensation system is used to study the feasibility of direct immersion cooling of a CPU. The design of an efficient controller requires a good understanding of the working principles of the Peltier cells. So, a secondary objective is to characterize the Peltier cells under real working conditions, namely their internal properties and the dynamic response. This is expected to be useful to provide alternative methods and guiding values to characterize the internal properties of the cells in works focused on the application and not on the fundamental research, as these methodologies are still sparsely reported in the literature. Such characterization of the system is important for a closed-loop control and is vital to an open-loop control, so it is an important task to accomplish. A PID controller was designed to control the amount of cooling the Peltier cells provide. From the experimental procedures followed, results show that the internal properties of Peltier cells are within the range described in the literature and follow the same behaviour. Its dynamic response allowed to gain a sensibility of the limiting values and how the system responded. The PID controller showed very good results that were within the requirements previously proposed. A final test of 72 hours under 100% of CPU Load was made to study the feasibility of direct immersion cooling and the condensation system. The results obtained show that the combination of direct immersion cooling with the condensation system developed is indeed feasible.

Keywords

Peltier cell, PID Controller, Direct Immersion Cooling, CPU, Arduino, Condensation
Resumo

Este trabalho propõe o desenvolvimento e controlo de um Sistema de condensação usando células de Peltier. O sistema de condensação é usado para estudar a viabilidade do arrefecimento de um processador por imersão directa. Para desenvolver um controlador eficiente, é preciso ter um bom conhecimento dos princípios de funcionamento das células de Peltier. Portanto, um objectivo secundário é a caracterização das células de Peltier em condições reais, nomeadamente as suas parâmetros internos e resposta dinâmica. Com isto é esperado obter-se algum conhecimento e valores de referência que permitam caracterizar os parâmetros internos da célula numa aplicação real e não apenas através de teoria. Esta caracterização é relevante para desenhar um controlador em malha-fechado mas é principalmente importante para desenhar um controlador em malha-aberta, portanto é uma caracterização relevante que deve ser feita. Um controlador PID foi desenvolvido para controlar o arrefecimento as células de Peltier produziam. Através da realização dos procedimentos experimentais, foram obtidos resultados que mostram que os parâmetros internos estão dentro da gama descrita na literatura e que têm as mesmas dependências em relação a certas variáveis. Além disso a resposta dinâmica permitiu ganhar uma maior sensibilidade de alguns valores limites e a resposta que sistema dava. Os resultados do teste do controlador PID demonstram que efectivamente o controlador consegue seguir muito fielmente a referência imposta tendo em conta os requisitos previamente definidos. Um teste final de 72 horas com a carga máxima do processador foi feito para demonstra a viabilidade do arrefecimento por imersão directa e sistema de condensação. Os resultados mostram que de facto que a combinação do sistema de arrefecimento por imersão directa com o sistema de condensação é de facto uma solução viável.

Palavras-chave

Células Peltier, Controlador PID, Arrefecimento Imersão directa, Processador, Arduino, Condensação
# Table of Contents

Acknowledgements ........................................................................................................... v
Abstract .......................................................................................................................... vii
Resumo .......................................................................................................................... viii
Table of Contents ........................................................................................................... ix
List of Figures ................................................................................................................ xi
List of Tables .................................................................................................................. xiii
List of Acronyms ............................................................................................................ xiv
List of Symbols ............................................................................................................... xv
List of Software .............................................................................................................. xvi

1 Introduction .................................................................................................................. 1
  1.1 Overview and Motivation .......................................................................................... 2
  1.2 Objectives .............................................................................................................. 5
  1.3 Contents ................................................................................................................ 5

2 State of the Art ............................................................................................................. 6
  2.1 Electronic Cooling Techniques .............................................................................. 7
  2.2 Peltier Cells State of the Art ................................................................................ 9

3 Pool Boiling as a cooling technique .......................................................................... 12
  3.1 Indirect and Direct Contact cooling ..................................................................... 13
  3.2 Boiling Curve and regimes and Condensation ................................................... 16
  3.3 Condensation ...................................................................................................... 19
  3.4 Cooling configurations using phase change ..................................................... 23

4 Peltier Cells ............................................................................................................... 25
  4.1 Introduction ......................................................................................................... 26
  4.2 Peltier cells in various applications: advantages and drawbacks ............... 26
List of Figures

Figure 1.1 – Conceptual Design .................................................................4
Figure 3.1 – Indirect Contact ....................................................................15
Figure 3.2 – Direct Contact........................................................................15
Figure 3.3 - Drew and Muller Experiment (Black) and Nukiyama Curve (Red arrows) ..................................................18
Figure 3.4 – Nomenclature for filmwise condensation on a vertical plane surface [44] ..................................................21
Figure 4.1 – Single N-type pellet ...............................................................28
Figure 4.2 – Single P-type pellet ...............................................................28
Figure 4.3 – Multiple P-type pellets connected in parallel .........................29
Figure 4.4 – Single N-P-type pellet ..........................................................30
Figure 4.5 – Multiple N-P-type pellets ......................................................30
Figure 4.6 – Typical Configuration of a Peltier device [56] .........................30
Figure 4.7 – Current Flowing through N-P junction ..................................31
Figure 4.8 – Heat flow through a Peltier cell ..........................................32
Figure 5.1 – Conceptual design. The numbers identify each of the aforementioned essential components of the system ........................................................................36
Figure 5.2 – Multicomp MCPF-127-14-11-E ............................................38
Figure 5.3 – Zalman CNPS7500-AiCu LED .............................................40
Figure 5.4 – Setup developed to characterize the Peltier cells ....................41
Figure 5.5 – Potentiometer and Thermocouples placement in the resistance ............................................................41
Figure 5.6 – Hewlett Packard 6274B DC Power Supply and Rear-Panel connections ....................................................43
Figure 5.7 – Arduino Due .........................................................................44
Figure 5.8 – MAX31855 Pin Configuration ................................................46
Figure 5.9 – Final Setup ............................................................................47
Figure 5.10 – Dimensions of the final pool ...............................................48
Figure 5.11 – Dimensions of the final pool ...............................................48
Figure 5.12 - Detail of the Coupling Fan/Peltier/Insulation/Aluminum wall ............................................................49
Figure 6.1 - Absolute temperature of the cold surface for 1A of current ..........59
Figure 6.2 – Dynamic response for 1A of current .......................................60
Figure 6.3 – Temperature difference between both surfaces of the Peltier cell for 1A of current .................................61
Figure 6.4 – Absolute temperature of the hot surface for 1A of current .........61
Figure 6.5 - Dynamic response for 2A of current .......................................62
Figure 6.6 - Temperature difference between both surfaces of the Peltier cell for 3A of current .................................62
Figure 6.7 - Dynamic response for 3A of current .......................................62
Figure 6.8 - Dynamic response for 4A of current .......................................63
Figure 6.9 - Dynamic response for 5A of current .......................................63
Figure 6.10 - Dynamic response for 6A of current .......................................64
Figure 6.11 - Dynamic response for 7A of current .......................................64
Figure 6.12 - Dynamic response for 8A of current .......................................64
Figure 6.13 - Dynamic response for 8.5A of current ....................................64
Figure 6.14 - Absolute temperature of the hot surface for 8.5A of current ......64
Figure 6.15 - $\Delta T$ for $Q_{imp} = 0W$, for each of the currents tested ............64

---

xi
Figure 6.16 – $Rm$ vs $\Delta T$ .............................................................................................................65
Figure 6.17 – Relation between Seebeck Coefficient and $\Delta T$ between both surfaces of the Peltier cell ........................................................................................................................................66
Figure 6.18 - Relation between Thermal Conductance and $\Delta T$ between both surfaces of the Peltier cell ........................................................................................................................................67
Figure 6.19 – $Kp=5.0; \, Ki=0.01; \, Kd=1.0$ for $TCref = 28^\circ C$ .................................................................................................................................68
Figure 6.20 - $Kp=0.2; \, Ki=0.01; \, Kd=1.0$ for $TCref = 28^\circ C$ .................................................................................................................................68
Figure 6.21 - $Kp=1.0; \, Ki=0.01; \, Kd=1.0$ for $TCref = 28^\circ C$ .................................................................................................................................69
Figure 6.22 – Comparison of the proportional terms ........................................................................69
Figure 6.23 - $Ki=0.05; \, Kp=1.0; \, Kd=1.0$ for $TCref = 28^\circ C$ .................................................................................................................................70
Figure 6.24 - $Ki=0.002; \, Kp=1.0; \, Kd=1.0$ for $TCref = 28^\circ C$ .................................................................................................................................70
Figure 6.25 - $Ki=0.01; \, Kp=1.0; \, Kd=1.0$ for $TCref = 28^\circ C$ .................................................................................................................................70
Figure 6.26 - Comparison of the integrative terms ........................................................................70
Figure 6.27 - $Kd=5.0; \, Kp=1.0; \, Ki=0.01$ for $TCref = 28^\circ C$ .................................................................................................................................71
Figure 6.28 - $Kd=0.2; \, Kp=1.0; \, Ki=0.01$ for $TCref = 28^\circ C$ .................................................................................................................................71
Figure 6.29 - $Kd=1.0; \, Kp=1.0; \, Ki=0.01$ for $TCref = 28^\circ C$ .................................................................................................................................71
Figure 6.30 - Comparison of the derivative terms ........................................................................71
Figure 6.31 – PID Controller test with $TCref = 15^\circ C$ .................................................................................................................................72
Figure 6.32 – Final test of 72 hours under CPU full load ....................................................................73
Figure 6.33 - CPU Temperature .......................................................................................................73

Figure A.1. Comparison between the Gamma PDF and the PDF equivalent modified histogram obtained from the Gamma RNG ($\beta=9, \lambda=100$). Erro! Marcador não definido.
Figure B.1. BR versus User Scenario (G). Erro! Marcador não definido.
List of Tables

Table 3.1 - Convective Heat Transfer Coefficient for several processes ........................................16
Table 5.1 - Multicom MCPF-127-14-11-E Characteristics .............................................................39
Table 5.2 - Remote programming coefficients ..............................................................................43
Table 5.3 - MAX31855 Specifications ............................................................................................45
Table 5.4 - MAX31855 Pin Description ..........................................................................................46
Table 5.5 - Thermophysical properties of the liquids used in the present study, taken at saturation, at 1.013x10^5Pa........................................................................................................50

Table A.1. Observation parameters and MSE of each RNG.......... Erro! Marcador não definido.
### List of Acronyms

<table>
<thead>
<tr>
<th>Acronym</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CPU</td>
<td>Central Processing Unit</td>
</tr>
<tr>
<td>IC</td>
<td>Integrated Circuit</td>
</tr>
<tr>
<td>TEC</td>
<td>Thermoelectric Cooler</td>
</tr>
<tr>
<td>emf</td>
<td>Electromotive force</td>
</tr>
<tr>
<td>MTBF</td>
<td>Mean time between failures</td>
</tr>
<tr>
<td>C.O.P.</td>
<td>Coefficient of Performance</td>
</tr>
<tr>
<td>DC</td>
<td>Direct Current</td>
</tr>
<tr>
<td>AC</td>
<td>Alternate Current</td>
</tr>
<tr>
<td>PWM</td>
<td>Pulse-Width Modulation</td>
</tr>
<tr>
<td>PID</td>
<td>Proportional Integrative Derivative</td>
</tr>
</tbody>
</table>
List of Symbols

\( h \) \hspace{1cm} \text{Convective Heat Transfer Coefficient}
\( \Delta T \) \hspace{1cm} \text{Temperature difference}
\( I \) \hspace{1cm} \text{Current}
\( V \)
List of Software

Arduino IDE
TEC Calculator
Everest
OriginPro 8.0
This chapter gives a brief overview of the work, as well as motivation and objectives.
1.1 Overview and Motivation

Since the birth of electronic technology, the heat flux produced by electronic devices has increased and this trend is expected to continue. In 1965, co-founder of Intel Gordon E. Moore stated that the number of components in an integrated circuit (IC) would approximately double every two years [1]. This trend, which was later known as Moore's law has been correct by half a century and is expected to continue until 2020 according to Kanellos [2]. Moore also posed the question “Will it be possible to remove the heat generated by tens of thousands of components in a single silicon chip?”

Since the end of the seventies, processors have improved their performance by 35% each year [3], while the size of integrated circuits has decreased [4]. However, this led to an increase in the power dissipated by electronic devices. This approach of reducing the size and increasing the frequency of operation, thus increasing the power dissipated has been possible until 2004. From this moment, the existing architectures were unable to dissipate to heat generated, so that new architectures have been adopted to continuously increase the performance while maintain the power dissipated. These architectures mainly consisted in distributing the workload across multiple less powerful processors. Computer architectures nowadays continue to find new ways to increase performance by distributing the workload and thus distributing the heat dissipation. However, the increase of heat generated by the processors is inevitable. This trend led Hennessy and Patterson [3] to state that thermal management of electronic devices would be, in the near future, the biggest limitation in the development of new processors. Additionally, a constant temperature below the junction temperature is required, which is approximately 85ºC for reliable operation and increased electronic device lifespan. Bar-Cohen et al. [5] alert for the performance degradation and reliability that this increase in heat dissipation can cause. Moreover, Tonapsi et al. [6] state that an increase by 10ºC in the temperature is enough to reduce the device life by half, while Paik et al. [7] state that an increase by 15ºC can increase time response (interconnect delay) from 10% to 15%. In line with this, the development of new techniques to cool down electronics becomes crucial. Cader et al. [8], state that the conventional air cooled systems have trouble accompanying the heat flux generated by constant increase of clock frequency and number of transistors.

In recent years, various promising techniques for electronic cooling have been studied. In this work the feasibility of Direct Immersion Cooling in a dielectric liquid is tested, which addressed the liquid phase change. Two-phase cooling techniques, in which there is a phase change of the liquid, have much potential because they have a higher convective heat transfer coefficient than conventional computer cooling techniques (eg. air cooling and water cooling). As the name implies, the heated surface which in this case is the Central Processing Unit (CPU) is immersed in a fluid. For this to be possible the fluid must have dielectric properties. To take full advantage of this technique, the fluid used must have a lower boiling point than the heated surface temperature. At a given temperature difference between the boiling point of the fluid and the temperature of the surface, the liquid starts to boil. As will be explained later, when boiling occurs there is a phase change in which the convective heat transfer coefficient rises exponentially allowing higher heat fluxes to be removed.
However, in these techniques the boiling liquid vaporizes very fast and will be lost if it is not properly condensed. Given the particular properties that these liquids must have, the feasibility of such cooling systems strongly depends on an efficient condensation system. This way, losses of the fluid are avoided and the system can continuously work for long periods of time.

The vapour will only condense in a stable condition for a well-defined temperature difference between the boiling point of the fluid and the temperature of the surface responsible for the condensation of the fluid. However, the CPU works in transient conditions for which the heat flux dissipated may change significantly along time. It is possible that for some periods of time the CPU may work under full load and generate its Thermal Design Power (TDP). This is usually given by the manufacturer and corresponds to the maximum heat power released by the CPU.

When the heat flux generated by the CPU changes, i.e. the pace at which the fluid evaporates, the temperature of the surface responsible for condensation must also be adjusted, to assure that the temperature difference is high enough to promote the vapour condensation. Hence, the good performance of the condensation system depends on how well it can adapt the temperature of the surfaces responsible for condensation to the different heat fluxes created by the CPU during its working period. So, the key for a good performance of the condensation system lays in the accurate control of that temperature.

In this context the main purpose of this work is to develop a controlled condensation system using Peltier cells, which can fix the temperature of the surface responsible by the condensation of the fluid, accordingly to the power supplied to them. This adjustment is made taking into account the variations in the heat dissipation associated to different CPU loads, which occur during its functioning. Despite their relatively low efficiency, Peltier cells were chosen to include the condensation system as they allow precise temperature control, independently of the ambient temperature which is, as aforementioned, one of the biggest limitations of conventional cooling techniques. The condensation system is integrated in a pool boiling cooling strategy. The conceptual design for the system is represented in Figure 1.1. The CPU, identified by number 1, is immersed in a pool, identified by number 2, filled with a dielectric fluid (the fluid used here is HFE-7000, as further explained). As the temperature difference between the CPU and the boiling point of HFE-7000 (34ºC) increases, boiling starts to occur and HFE-700 evaporates. The vapour is transported due to a gradient density and it comes in contact with the ceiling of the pool, which must be at a lower temperature than the HFE-7000 saturation temperature, so it can condensate. The temperature of the ceiling of the pool is fixed by the Peltier cell, identified by number 3. The Peltier cell allows to precisely fix a temperature accordingly to the current supplied to it. On top of the system is the heatsink, identified by number 4, and the fan, identified by number 5, which are responsible for dissipating the heat flux created by the CPU and the Joule effect generated by the Peltier cell.

The Peltier cells may seem useless, given that at this stage of the work they could not be completely removed from the cooling components and are actually being used to cool the cells. As it will be explained later, in Chapters 3 and 5, the heatsink cools the CPU by conduction and the fan cools the heatsink by forced convection of the air. So, in this context we have still the physical...
limitation imposed by the temperature of the ambient air. However, when this temperature is above the saturation point of the dielectric fluid, condensation will not occur. If the pool is not sealed, the fluid is lost. If the pool is sealed, the fluid is not condensed, so the pressure inside the pool may rise up to dangerous values. In addition, the boiling point of most liquids, including HFE7000 increases with pressure, so the temperature of the liquid will increase until values which do not assure a safe temperature for the CPU to work. In this context, the Peltier cells solve both these issues, while allowing a precise control of the temperature of the condensation surface, almost independently from the ambient temperature.

Furthermore, if the control of the Peltier cells is robust enough, it may allow the system developed here to operate in any other applications requiring cooling and a precise control of the temperatures (which does not necessarily need to include condensation).

Figure 1.1 – Conceptual Design
1.2 Objectives

Following the context presented above, the objective of this work is to design a controlled condensation system using Peltier cells. This work is integrated in a project whose objective is to study the feasibility of Direct Immersion Cooling and particularly pool boiling as a commercial cooling system. As aforementioned the system to be developed must fix the temperature of the surface responsible by the condensation of the fluid, accordingly to the power supplied to the Peltier cells. This adjustment is made taking into account the variations in the heat dissipation associated to different CPU loads.

The design of an efficient controller requires a good understanding of the working principles of the Peltier cells. So, a secondary objective is to characterize the Peltier cells under real working conditions, namely their internal properties and the dynamic response. This is expected to be useful to provide alternative methods and guiding values to characterize the internal properties of the cells in works focused on the application and not on the fundamental research, as these methodologies are still sparsely reported in the literature. Such characterization of the system is important for a closed-loop control and is vital to an open-loop control, so it is an important task to accomplish.

Although one cannot aim at the development of a fully operational cooling system, as this is a complex task, which is out of the scope of a single Master Thesis, a preliminary configuration is proposed and tested in a real application test, which consists in the cooling of a personal computer.

1.3 Contents

The present thesis is composed of 7 chapters. Chapter 1 introduces the context and Motivation for the present work and presents the objectives of this thesis. Chapter 2 provides a brief review of the literature in cooling techniques used in electronic cooling and as in Peltier cells. The latter includes fundamental studies on theoretical concepts, but also works concerning several applications of the Peltier cells. Chapter 3 deepens the basic heat transfer concepts which are required to understand the cooling techniques and some of the results which will be discussed later. Chapter 4 addresses the fundamental theoretical concepts governing the working principles of the Peltier cells, as well as benefits and drawbacks of using them for several purposes. Chapter 5 presents the experimental apparatus used and the experimental procedures followed. Chapter 6 discusses the results obtained by following the experimental procedures proposed. Finally, chapter 7 presents the conclusions that were taken from this work and as well as various suggestions of future work that can be performed to improve the system.
Chapter 2

State of the Art

This chapter provides a brief overview of the state-of-the-art electronic cooling and on Peltier Cells, if and what control systems were used.
2.1 Electronic Cooling Techniques

The need for new cooling techniques is driven by continuing increases in power dissipation of electronic parts and systems. In many instances standard techniques cannot achieve the required cooling performances due to physical limitations in heat transfer capabilities. These limitations are principally related to the limited thermal conductivity of the fluids and of the materials used to cool the processors (air is usually used for forced convection and copper is the material made to dissipate the heat by conduction) [9]. Due to stringent cost and reliability constraints, air-cooling will remain an important thermal management approach for many electronic products in the foreseeable future [10]. Although considerable performance improvements have taken place in the last decades, it is generally accepted that traditional air-cooling techniques are about to reach their limit for cooling of high-power applications. For instance, Lasance et al. [9] state that with standard fans a maximum heat transfer coefficient of maybe $150 \frac{W}{m^2K}$ can be reached with acceptable noise levels. However, several commercial brands in the computer cooling industry continuously release new designs. Air cooling is traditionally associated with the use of heat sinks, which are the most commonly-employed, cost-effective electronics thermal management hardware. Exception made to underwater or marine applications, heat removed from electronic systems is ultimately dissipated to the air [11]. Heat sinks’ function is mainly to extend the surface area of heat dissipating surfaces through the use of fins. Their design and analysis is one of the most extensive research areas in electronic cooling. Advances in heat sink cooling performance have been achieved through progress in manufacturing technology and to lesser extent, fan design, thereby resulting in more efficient heat removal [10]. However, these techniques are always limited by the temperature of the ambient air.

Cooling electronic chips does not only address the dissipation of the heat, but it also requires the junction temperature to be maintained within an acceptable range, typically 85-100ºC [12]. Conventional air cooled designs are no longer adequate to remove the actual heat fluxes, which can be much higher than the 150W/m2K and are not capable to keep the junction temperature within a safe range. Therefore, for a number of applications, air-cooling must be replaced or supplemented by other high performance compact cooling techniques [13]. There are several techniques which can be categorized as direct cooling. This context will be further explained in Chapter 3, but it is mainly related to the fact that the system to cool (e.g. the CPU) is in direct contact with the coolant fluid. Also, direct cooling is not a new concept. Already in the sixties, Bar-Cohen et al. [14] refer that direct application of fluids was used to cool macro electronics. However, this cooling strategy became more popular in the eighties after being used by big brands such as IBM. However, direct liquid immersion often implied only the replacement of air with a liquid, which usually has higher convection coefficients. However, benefices can be taken in terms of the convective coefficients, when phase change occurs. In this context Seok Ahn et al. [15] states that boiling is the most efficient heat transfer mechanism. They argue that boiling is an attractive option for tackling the thermal management issues, particularly
for cooling of microprocessors and high heat flux devices. There are several techniques that make use of materials phase change to cool down electronic components. Most of them use the boiling of a liquid to achieve higher heat fluxes. Some of these strategies include direct immersion cooling which is commonly known as pool boiling, micro-channels and spray or jet impingement. Direct immersion cooling is a well-established method for accommodating high heat fluxes backed by over thirty years of academic and industrial research [9]. Many researchers reported the enhancement of heat transfer by using newly materials or structures combined with pool boiling [15]. Boiling in micro-channel heat sinks is attractive for high-power performance electronics due to the high heat transfer rates that can be achieved. However, the physics of flow boiling in micro-channels, the flow patterns present, and the effect of micro-channel size on the boiling regimes have not been investigated extensively, particularly with dielectric fluids [16]. Micro-channel have been studied by Silverio et al. [17], Argawal [18] and many others. However, the system miniaturization in diverse applications raises the need to better comprehend the scale effects induced on convective heat transfer inside micro-tubes. Several reviews related to mini-channel and micro-channel heat transfer, pressure drop, critical heat flux, flow instabilities and flow patterns are available in the literature [19] and all agree that there is no uniformity in the experimental data.

Bostanci et al. [20] performed experiments to investigate spray cooling on micro-structured surfaces. At 500 $W/cm^2$, the increases in the heat transfer coefficient for micro-structured with protrusions and indentations were 112% and 49% over smooth surface, respectively. Mudawar et al. [21] have shown that spray impingement cooling is one of the most efficient technologies for heat flux removal per unit of fluid flow. However, even with significant number of studies performed on spray cooling, relatively little is known about the exact mechanisms of energy transport or the peak heat flux in these systems. Thus, to date, engineers have not had the necessary tools to design robust, predictable spray systems for broader applications [22].

Regarding the application of Peltier cells to electronic cooling, they were not much used because of their Coefficient of Performance (C.O.P.) of about 1, which is rather low when compared to household refrigerators and air conditioners is from 2 to 4. Their cooling capability may also be limited over 5 – 10 $W/cm^2$. This makes thermoelectric cooling generally not competitive. Lasance et al [9] state that despite the low efficiency, the application of areas are increasing and include infrared detector cooling, charge coupled devices, microprocessors, blood analysers, portable picnic coolers. The main characteristics are still the accurate control of temperature and the possibility of cooling below ambient temperature. Additionally, the hardware simplicity is an advantage when compared to high pumping and expanding works required with refrigerators. The small size required for the pumps and turbines or valves in the context of cooling applications is also a complex task that has not been successfully achieved yet. According to Lasance et al [9] since the cooling density of a Peltier cooler is inversely proportional to its length, scaling to smaller size is desirable. The material structure produced by conventional crystal growth techniques to obtain bismuth telluride thermoelectric materials impose significant limitations on thermoelectric element dimensions due to poor manufacturing yields. So, this may also limit the minimum possible dimensions of the thermoelectric. However, significant progress has been developed to overcome this obstacle. Marlow industries reported that new-fine grain micro-
alloyed bismuth telluride materials that do not suffer the element geometry limitation and can offer higher performance [23]. MicroPelt, a spin-off company from Fraunhofer and Infineon also sells promising thin films for near future claiming cooling of 160 W/cm².

Recently Cooler Master launched the V10 [24] which is a heat sink hybrid with fans and Peltier cell. This is composed of 10 heat pipes, 6 for the main body and 4 for the Peltier to maximise heat transfer. Dual PWM fan ensures huge airflow over the heat sinks. The Peltier cell is activated once CPU reaches extremes temperatures.

2.2 Peltier Cells State of the Art

Regarding Peltier cells formulation and applications, Riffat et al. [25] provide an extensive review of present and potential applications of thermoelectric devices from applications of Peltier cells as coolers, as devices for power generation, thermal energy sensors, aeronautics and space applications. The formulation of the theoretical concepts governing the working principles of the Peltier cells is extensively described in the literature [26, 27, 28, 29]. Palacios et al. [30] provides an analytical procedure to obtain parameters from performance curves of commercial thermoelectric modules. For a standard application it is not difficult to select the correct module looking at the performance values of appropriate family of modules. Then, it is possible to estimate the final behaviour of the application by using the performance curves (provided that the temperatures can be estimated correctly). However, for non-standard applications, such as those considered in the present work, the Peltier modules may work at atypical conditions, which are not considered in the performance curves. In this case, it is helpful to use an analytical model able to predict the behaviour of module. Alternatively, one must determine empirical approaches to characterize the cells working under those specific conditions. Although Palacios et al. [30] state that experimental measurements do not perfectly match the results estimated analytically, these measurements can be considered rather precise considering the difficulties for attaining accurate experimental measurements in a standard laboratory. In this context, the present work will also discuss methodologies to characterize the Peltier cells’ internal properties, making use of experimental approaches.

Alternatively to the experimental characterization of the Peltier cells, few authors attempted to develop numerical models to predict the internal properties of cells. For instance, Pérez-Aparicio et al. [31] present a finite element simulation of a commercial thermoelectric cell, working as a heat pump. The specifically developed finite element is three-dimensional, non-linear in its formulation (using quadratic temperature-dependence on material properties) and fully coupled, including the Seebeck, Peltier, Thomson and Joule effects. A thorough study of the distributions of voltage, temperatures and the corresponding fluxes is presented, and the performance of cell is compared with that of the manufacturer and with simplified analytical formulations, showing a good agreement. The concept is to define which variables need to be controlled in the design process of Peltier cells to improve its performance. Pérez-Aparicio concluded that the design variables that need to be controlled to design
a good thermoelectric cell are: length, electrical conductivity, and Seebeck coefficients. Pérez-Aparicio states that these results agree with already known facts: a good thermoelectric module needs a high Seebeck coefficient to maximise the Peltier effect. Moreover, a high electrical conductivity is desired to reduce Joule effect and a low thermal conductivity results in a reduced heat transfer. This author also tested the influence of the temperature-dependence of the material properties in the Peltier cell performance and concluded that for the studied thermoelectric cell, the decreasing temperature-dependence of the electrical conductivity is more relevant for the Coefficient of Performance than the Seebeck coefficient and specially of thermal conductivity and of the consideration of reduced contact in the soldering connections. Similar study was performed by Yamashita [32] in which he assumed that all of the thermoelectric properties are expressed by a quadratic function of temperature, which was confirmed experimentally. Cheng et al. [33] propose a three-dimensional theoretical model for predicting the transient behaviour of thermoelectric coolers. In his model, the thermoelectric cooler is divided in four major regions, namely, cold end (region 1), hot end (region 2) and the P-type and N-type thermoelectric elements (regions 3 and 4). The simulation model is adopted to perform a parametric study to investigate the effects of the parameters such as electrical current, cooling load per unit area, heat transfer coefficients on surfaces and geometrical parameters such as total area of heat sink and height of semiconductor elements. They concluded that the temperature of the hot end and the temperature difference between the hot and cold ends both increase with the applied current. They also found that the magnitude of the C.O.P. is rapidly decreased as the current is increased. Cheng et al. [33] also suggest that the convective heat transfer from the heat sink to ambient could be influential. The hot end temperature is remarkably reduced by increasing the convective heat transfer coefficient of the heat sink. The heat loss from the surfaces of the P-type and N-type elements causes reduction in the C.O.P. However, the temperature difference is slightly influenced by a change in the heat transfer coefficient. They also showed that the influence of an increase in element height is actually involved. Finally, Cheng et al. [33] also found that the temperature difference between the two ends increases with the length. They also observed that both the temperature of the hot and cold side ends increase with cooling load, and the value of C.O.P. linearly increases with the cooling load.

Huang et al. [34] studied the influence of the Thomson effect on the performance of a thermoelectric cooler. In this case, a one-dimensional thermal analysis for the performance of thermoelectric cooler was conducted under the influence of the Thomson effect, the Joule heating, the Fourier’s heat conduction, and the radiation and convection heat transfer. The temperature distribution and cooling power were analytically derived. For the cases in which the Thomson effect is important, (i.e when the ratio of the Thomson heat to the conduction heat and the ratio of Joule’s effect to the Thomson heat, play non-negligible roles), both temperatures distribution and the cooling power are affected by the Thomson effect. The fraction of both Fourier’s conduction heat and Joule’s heat that flow back to cold side can be significantly reduced. Consequently, higher values of maximum temperature difference can be attained and the allowable heat load, providing that the thermoelectric cooler has P-type semiconductor material with the positive Thomson coefficient, is maxima.

Up to now, the reviewed studies are focused on the fundamental study of the internal properties of the cells. Regarding the application of Peltier cells as a thermal control of various
surfaces, it is worth mentioning the work of Deng et al. [35, 36] in which they propose a robust fault tolerant thermal control system of an aluminium plate with a Peltier Cell. This control system ensures that the control loop system remains insensitive to uncertain and random faults. Furthermore, it can tolerate some possible detrimental environment impacts.

Maruyama et al. [37] propose the development of a precise-temperature-controlled cooling apparatus for medical application using Peltier effect. In this study, a Peltier cryoprobe for dermis treatment and flexible cryoprobe for cryosurgery for deep region of human body were developed, based on the Peltier effect. The proposed apparatus has enough good performance to necrotize target diseased cells precisely. The proposed flexible cryoprobe is composed of a resin tube flexible enough to treat the deeper parts of the human body with a catheter. A Peltier element is attached at the top of the probe for active heat transfer control of the cooling tip. Cooling experiments were conducted and the performance of the cryoprobe was evaluated. The authors report that the cryoprobe could achieve temperatures as low as -43°C at the tip. The motivation for this study is that the conventional cryoprobes generally have a high cooling ability, enough to freeze and destroy the disease part, but cannot control the cooling rate precisely, because the cooling rate depends on refrigerative properties. Due to poor temperature control, the organ near the diseased part can get damaged. The results of this study were a cryoprobe which can control cooling and heating of target accurately by utilizing Peltier effect and boiling of liquid nitrogen. From animal experiments, it was confirmed that the cryoprobe has enough good cooling performance to freeze skin and destroy skin cells.

Another interesting work using Peltier cells is reported by Morimitsu and Katsura [38, 39]. These authors analysed an observer-based thermal control system of Peltier device. The objective of this study is to use a Peltier cell, which is a suitable device to produce heat transfer, to induce thermal sensations, i.e., utilizing the device for haptics. Haptics is an academic field which deals with the transmission of touch sensation. In the present industry of communication engineering, audio and visual information are the most transmitted. However, humans can not only hear and see, but also smell, taste, and feel tactile sensation. Haptics aims to present touch sensation which can become the third multimedia information to the operator. The idea behind transmitting thermal sensation is that temperature and heat flow are very important information for human actions. In this case, by touching a Peltier cell, the device would be able to read our temperature and heat flow and this information can be transmitted across the network to other point and inversely reproduce the same sensation.

Recently, Oven industries released the 5R6-900 which is a new temperature controller [40]. 5R6-900 is a solid state MOSFET bidirectional compact ramp and soak benchtop temperature controller for Peltier cells with an internal power supply, full H bridge and is capable of load currents up to 10A User friendly PC programmable via the electrically isolated RS232 com port. The functions of this product are very similar those proposed in the present.
Chapter 3

Pool Boiling as a cooling technique

This chapter deepens the basic heat transfer concepts that are required to understand the cooling techniques. Particular emphasis is given to a cooling strategy using liquids phase change. Hence, section 3.1 introduces the heat transfer processes occurring at direct and indirect cooling techniques. Afterwards, the basic concepts on pool boiling are revised in section 3.2, which are vital to understand how the boiling of a liquid can be used as a cooling technique. The description of the possible configurations of cooling systems using liquids phase change is discussed in section 3.3, which also analyses advantages and disadvantages of several cooling configurations using phase change.
3.1 Indirect and Direct Contact cooling

Most modern day processors have some interface between the central processing unit (CPU) and its surrounding. This interface is usually called heat spreader and two of its most important functions are to physically protect the CPU and to increase the heat exchange area. Heat can be exchanged by three different physical mechanisms: conduction, convection and radiation. The heat transfer by conduction is associated to the diffusion of energy occurring by atomic and molecular activity, when a temperature gradient exists. Hence, during conductive heat transfer there is not a macroscopic motion of mass, but instead, the heat is transferred by diffusion from the region with highest temperature to that with lowest temperature. The convective heat transfer is the combined effect of diffusion with advection, being the latter related to the heat that is transferred by the motion of a quantity of mass. Finally, radiative heat transfer is related to the energy that is emitted by the matter, at a specific finite temperature.

By definition, the heat flux is the rate of heat that is transferred per unit area, being this area perpendicular to the direction of the flux. Thus, the heat flux \( \dot{q} \) (W/m\(^2\)) is proportional to the temperature gradient:

\[
\dot{q} = -kA\frac{dT}{dx}
\]

(3.1)

where \( k \) [W/(m.K)] is the thermal conductivity of the material (i.e. it is a property of the material, which can be in solid, liquid or vapor phase) and the signal minus is used to identify that the heat is transferred from the highest to the lowest temperatures. In steady state, the rate of heat \( \dot{Q} \) that is transferred by conduction through a surface (e.g. the heat spreader) is given by:

\[
\dot{Q} = -kA\frac{\Delta T}{L}
\]

(3.2)

being \( A \) the area of the heat spreader and \( L \) its thickness. The heat spreader is in direct contact with the CPU, so the heat that is dissipated by the CPU is diffused to the heat spreader by conduction and only afterwards is removed from the heat spreader. Hence, most computer cooling systems cool the heat spreader, so that the categorization of the cooling techniques in direct or indirect cooling depends if the heat spreader is in direct or indirect contact with the cooling system.

Indirect cooling systems use an additional thermal interface which cools the heat spreader by conduction. However this thermal interface needs to also to be cooled, resorting to forced air convection or systems that use some kind of fluid. Whichever the system used, the thermal interface is cooled by convection by the fluid (gas or liquid). In direct cooling this additional thermal interface does not exist, so the cooling fluid is directly in contact with the heat spreader. The rate of heat that is removed from the surface (of the heat spreader or of the thermal interface) by the fluid is given by the Newton’s cooling law:
\[ \dot{Q} = hA(T_s - T_f) \]  \hspace{1cm} (3.3)

where \( h \) [\( W/(m^2.K) \)] is the convective heat transfer coefficient (which, contrarily to the thermal conductivity, is not a property of the material), \( A \) is the surface area, \( T_s \) is the surface temperature of the heat spreader or of the thermal interface and \( T_f \) is the temperature of the fluid.

Indirect and direct cooling can be schematically represented as depicted in Figure 3.1 and Figure 3.2, respectively. Following these figures it is relevant to introduce the concept of thermal resistance. This term implicates an analogy between heat exchange and the flowing of electrical current. Reminding eq. (3.2) and considering that the temperature difference \( \Delta T \) is analogous to the current and that the heat transfer rate is the analogous of the electrical tension, the thermal resistance by conduction is defined as:

\[ R_{\text{cond}} = \frac{\Delta T}{\dot{Q}} = \frac{L}{kA} \]  \hspace{1cm} (3.4)

Similarly, a convective heat transfer resistance can be defined as:

\[ R_{\text{conv}} = \frac{T_s - T_f}{\dot{Q}} = \frac{1}{hA} \]  \hspace{1cm} (3.5)

There is a third type of thermal resistance that plays an important role in heat exchange. This is referred to as Contact Resistance and it is due to roughness on the surface that creates cavities, most of the time filled with air. The usual solution to decrease the contact resistance consists in applying on these cavities a fluid with higher thermal conductivity than that of the material used.

The concept of thermal resistance is relevant because it allows us to analyse the problem of heat transfer as an analogy of an electrical circuit. As matter of fact, thermal resistances can be associated in parallel or series just as electrical resistances. The association of thermal resistances in series equals to the sum of their resistances while the association of thermal resistances in parallel equals the sum of the inverse of their value

\[ R_{\text{series}} = R_1 + R_2 \]  \hspace{1cm} (3.6)

\[ \frac{1}{R_{\text{parallel}}} = \frac{1}{R_1} + \frac{1}{R_2} \]  \hspace{1cm} (3.7)

As shown in Figure 3.1, the use of indirect cooling systems introduces an additional thermal conduction resistance between the heat spreader and the thermal interface. This is pertinent if we analyse heat transfer equation for the entire system (eq. 3.7). The heat exchange depends on the global thermal resistance and the temperature difference between the CPU and ambient temperature. The ambient temperature is actually a limiting value for most of the current cooling systems. This is obvious when the cooling fluid is air. When other fluids are used (e.g. liquids), the heat that they remove from the heat spreader or from the thermal interface is usually exchanged to the ambient, for instance using a radiator.
In computer cooling, the goal is to reduce the CPU temperature and this is achieved by reducing the global thermal resistance.

As seen in Figure 3.1, the global thermal resistance of an indirect cooling system corresponds to the sum of each resistance resulting in \( R_{\text{Global}} = R_{\text{Cond}_1} + R_{\text{Cond}_2} + R_{\text{Conv}} \), while in direct cooling systems (Figure 3.2) the absence of the thermal interface results in a lower global thermal resistance \( R_{\text{Global}} = R_{\text{Cond}_1} + R_{\text{Conv}} \). From this simple analysis one can conclude that direct cooling systems have higher potential to achieve lower CPU temperatures because of the lower global thermal resistance.

Back to Figure 3.1 and Figure 3.2, it can be seen that the thermal convection resistance is present independently of the technique used to cool down the system. When cooling a system by
convection, this can be either forced, in which the fluid motion is driven by external forces, or natural, in which the motion is induced by density differences caused by temperature differences of the fluid. Besides the presence of a larger or lower thermal resistance, the “better” or “worse” performance of the cooling systems is strongly related to the heat transfer coefficient, given the important role of convection in the cooling process. Actually, the noticeable higher performance of systems that use water instead of air (e.g. Watercooling) is due to the fact that the values of $h$ for liquids such as water are significantly larger than those of gases. The heat transfer coefficient also depends on the velocity of the fluid so that $h$ of forced convection systems is larger than that obtained in free convection systems. Representative values of the convective heat transfer coefficient are given in Table 3.1. The much higher value of $h$ presented for phase change processes (boiling or condensation) in comparison to the values obtained for free or forced convection will be explained in the following section, but in line with the discussion presented so far, such high value foresees the great potential of using phase change processes to cool the processors.

<table>
<thead>
<tr>
<th>Process</th>
<th>$h \left( \frac{W}{m^2 \cdot K} \right)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Free convection gas</td>
<td>2.25</td>
</tr>
<tr>
<td>Free convection liquid</td>
<td>50-1000</td>
</tr>
<tr>
<td>Forced convection gas</td>
<td>25-250</td>
</tr>
<tr>
<td>Forced convection liquid</td>
<td>100-20,000</td>
</tr>
<tr>
<td>Boiling or Condensation</td>
<td>2500-100,000</td>
</tr>
</tbody>
</table>

### 3.2 Boiling Curve and regimes and Condensation

Vaporization of a substance is the phase transition from liquid to gas phase. There are two types of vaporization: evaporation and boiling. Boiling generally refers to the process that occurs along solid surfaces submerged in the liquid and is characterized by the creation of vapour bubbles while evaporation usually occurs at liquid/vapour interface.

Boiling typically starts when the heated surface temperature is above the liquid saturation temperature (the boiling point) by $\Delta T$ large enough to promote the creation and departure of vapour bubbles from the heated surface.

For a surface experiencing boiling heat transfer, the variation of heat flux results in a characteristic temperature response at the surface, reflecting a progression through particular regimes...
of ebullient heat transfer. In 1934, Shiro Nukiyama [41] was the first to define the different boiling regimes resulting in the Nukiyama curve which relates the heat flux and $\Delta T$ between the surface temperature and liquid saturation temperature.

He conducted experiments with a horizontal nichrome wire (melting point: 1500K) at atmospheric pressure, immersed in saturated water. The heat flux was determined by the measurement of the electrical current $I$ and potential drop $V$. The wire temperature was measured from the change of the electrical resistance due to temperature variation.

Nukiyama noticed that as he increased the power given to the wire, bubbles started to form at $\Delta T$ of roughly 5°C. He noticed the power supplied to the wire could be increased greatly without a large increase in temperature until point C, which he defined as where the critical heat flux occurred. As he continued to increase the power supplied, he observed a sudden decrease in temperature and the wire reached the melting point (point E).

While repeating the experiment with a platinum wire, Nukiyama was able to obtain the curve remarked by red arrows in Figure 3.3. As it can be observed, Nukiyama obtained a hysteresis phenomenon due to the fact that the curve obtained is different whether one gradually increases or decreasing the heat flux. This hysteresis was due to the Power Control mechanisms used by Nukiyama. Therefore, increasing the heat flux, the resulting curve is defined through the points A-B-P-C-E, while decreasing the heat flux results in the curve defined through points E-D-A.

Nukiyama believed that a method to control $\Delta T$, instead of power controlled method, would yield a better curve. Later in 1937, Drew and Muller [42] performed the experiment using a steam pipe and obtained a curve similar to the black one reported in Figure 3.3.

Assuming a temperature controlled system, the following pool boiling regimes can be identified:

**Natural Convection**

The underlying physical mechanism of region 1 of the boiling curve demonstrated in Figure 3.3 is natural convection. While $\Delta T$ is lower than that observed in point A, the fluid motion is mainly governed by natural convection effects. i.e., the fluid near to the heated surface is heated, becomes less dense and rises due to buoyancy. The surrounding, cooler fluid then moves to replace it being in turn heated and forming a convection current. This process transfers the heat energy from the heated surface from the bottom to the top of the pool. The process is characterized by single-phase natural convection from the hot surface to the saturation fluid without formation of bubbles on the surface.

**Nucleate Boiling**

Above a certain $\Delta T$ (point A), vapour bubbles appear on the heated surface. This is referred as the onset of nucleate boiling. The bubbles form on scratches or cavities on the surface that contain pre-existing vapour nuclei. In liquids with low surface tension, the onset of nucleation may be delayed. For these fluids, a reduction in the surface temperature occurs while the heat flux remains constant due to a sudden inception of large number of cavities. This difference in the wall temperature before
and after boiling incipience is called “incipience overshoot”.

After this, a dramatic increase in the boiling curve is observed which corresponds to Region II in Figure 3.3. In the partial nucleate boiling regime, isolated bubbles are released from randomly active sites on the wire surface. This release of the bubbles from the surface induces a considerable motion near the surface, resulting in a direct heat transfer from the surface to liquid leading to a substantially increase in $h$ and $\dot{q}''$.

![Figure 3.3 - Drew and Muller Experiment (Black) and Nukiyama Curve (Red arrows)](image)

The transition from isolated bubbles to fully developed nucleate boiling (region III) occurs when bubbles at a given site begin to emerge in a vertical direction. In this phase, the bubbles are released in the form of jets and due to the densely formation of bubbles, they interfere between each other causing a decrease of the heat transfer coefficient. Point P of Figure 3.3 corresponds to an inflection in the boiling curve in which the slope of heat transfer coefficient reaches its maximum value. After this point, even though $\dot{q}''$ continues to increase there is a decrease in the slope of the boiling curve. $\dot{q}''$ continues to increase until point C which is called critical heat flux region and is the upper limit of the nucleate boiling region, at which the heat transfer is maximum. For cooling purposes, the critical heat flux is the limiting value to work. As one passes this region, the heat flux decreases dramatically, so that the system to cool can be easily damaged by overheating (the so called system burnout).
### Transition Boiling

The region IV called transition boiling is the phase resulting from the mix of features between nucleate boiling and film boiling. Bubble formation is now so fast that a blanket of vapour forms on the surface. The fraction of film boiling over nucleate boiling increases with the increase of $\Delta T'$, but any given location on the surface can oscillate between one or the other. However, the conductivity of vapour is lower than a fluid and thus $h$ decreases with the increase of $\Delta T'$.

### Film Boiling

Region V is called Film Boiling which is represented by curve ED. At point D, referred as Leidefrost Point, the heat flux shows a minimum $q'_{\text{min}}$ and the fraction of vapour blanket is unitary. In this phase, heat exchange from the surface occurs by conduction and radiation through the vapour. In 1756, it was Johann Leidenfrost [43] who observed that a liquid in near contact with a mass significantly hotter than the liquid’s boiling point produces an insulating vapour layer keeping that liquid from boiling rapidly. As the surface temperature is increased, radiation through the vapour film becomes more significant and the $h$ increases with $\Delta T'$.

During boiling, an additional heat transfer quantity is removed by the liquid over the surface, which is related to the energy that is required to provide for the phase change. This amount of energy is proportional to $m h_{fg}$ where $m$ is the mass flow of liquid that turns into vapour and $h_{fg}$ is the latent heat of vaporization. This amount of energy can be quite high, particularly in certain fluids like water and it is the main reason for the high value of $h$, earlier depicted in Table 3.1 for boiling processes. Additionally, while the pressure is kept constant, the temperature of a liquid during phase change is kept constant, thus allowing good control on the temperature of the process. In this context, several cooling configurations have been explored within the last years, which try to take advantage of the latent heat. These configurations, which were summarized in the State of the Art, are now presented in more detail in the following section.

### 3.3 Condensation

Given that the system developed here is actually acting on the condensation of the vapour that is generated during pool boiling, it is relevant to introduce the condensation theory that is important to understand the design of the final setup, as well as the discussion of the results presented at the end of the work. When vapour temperature is reduced below its saturation value, the vapor condenses. In engineering applications, the vapor is condensed by bringing it into contact with a cold surface. The steam condensers for power plants are typical examples of the application of condensing steam [44]. If the liquid wets the surface, the condensation occurs in the form of a smooth film, which flows down the surface under the action of gravity. The presence of a liquid film over the surface constitutes a thermal resistance to heat flow. This is called filmwise condensation. Therefore, numerous
experimental and theoretical investigations have been conducted to determine the heat-transfer coefficient for film condensation over surfaces. The first fundamental analysis leading to the determination of the heat transfer coefficient during filmwise condensation of pure vapors (i.e., without the presence of non-condensable gas) on a flat plate and a circular tube was given by Nusselt in 1916. Over the years, improvements have been made to Nusselt’s theory of film condensation. However, exception made to the condensation of liquid metals, Nusselt’s original theory has been experimentally and is still widely used. The following paragraphs briefly describe Nusselt’s theory of film condensation of pure vapors on a vertical plate.

Considering the condensation of a vapor on a vertical plate, as represented in Figure 3.4, where \( x \) is the axial coordinate, measured downward along the plate, and \( y \) is the coordinate normal to the condensing surface. The condensate thickness is represented by \( \delta \equiv \delta(x) \). This condensation problem was first analyzed by Nusselt under the following assumptions:

1. The plate is maintained at a uniform temperature \( T_w \) that is less than the saturation temperature \( T_s \) of the vapor.
2. The vapor is stationary or has low velocity, and so it exerts no drag on the motion of the condensate.
3. The downward flow of condensate under the action of gravity is laminar.
4. The flow velocity associated with the condensate film is low; as a result, the flow acceleration in the condensate layer is negligible.
5. Fluid properties are constant.
6. Heat transfer across the condensate layer is by pure conduction, hence the liquid temperature distribution is linear.

The velocity distribution \( u(y) \) at any location \( x \) across the condensate layer can be determined from a force balance on a volume element, as shown by the shaded area in Figure 3.4. Equating the shear force upward to the buoyancy force acting downward, this force balance renders to:

\[
\mu \frac{du}{dy} = (\rho_l - \rho_v)(\delta - y)g dy dx
\]

or

\[
\frac{du}{dy} = \frac{g(\rho_l - \rho_v)}{\mu} (\delta - y)
\]

Where \( \delta \equiv \delta(x) \) is the thickness of the condensate layer at the position \( x \), \( \mu \) is the dynamic viscosity and the subscripts \( l \) and \( v \) refer to the liquid and vapor phases, respectively. Here one can assume zero shear stress at the liquid-vapor interface, because the vapor is considered almost stationary by assumption 2. At the wall surface, the liquid velocity is zero:

\[
u = 0 \text{ at } y = 0
\]

The integration of equation 3.11 subject to the boundary condition equation 3.12 gives the velocity distribution in the condensate layer:

\[
u(y) = \frac{g(\rho_l - \rho_v)}{\mu_l} (\delta y - \frac{1}{2}y^2)
\]

The mass flow rate of the condensate \( m(x) \) through any axial position \( x \) per unit width of the
The rate of heat released $dQ$ associated with the rate of condensation $dm$ is

$$dQ = h_{fg}dm$$

where $h_{fg}$ is the latent heat of condensation. The amount of heat released $dQ$ over the area $dx \cdot 1$ must be transferred across the condensate layer thickness $\delta$ by conduction, according to assumption 6. Therefore,

$$dQ = k_1 \frac{\tau_v - \tau_w}{\delta} dx \cdot 1$$

where $k_1$ is the thermal conductivity of liquid and $\tau_v$ and $\tau_w$ are the vapour saturation and wall surfaces, respectively. Introducing equations 3.16 and 3.18 into equation 3.17, one obtains the following differential equation for the thickness of the condensate layer:

$$\frac{d\delta}{dx} = \frac{\mu_2 k_1 (\tau_v - \tau_w)}{8\pi (\rho_l - \rho_v) h_{fg} \delta^3} \frac{1}{\delta^3}$$

The integration of equation 3.19 with the condition $\delta = 0$ and $x = 0$ yields the thickness of the condensate layer as a function of the position $x$ along the plate:
Since the relation for the thickness of the condensate layer was already established, the local heat transfer coefficient \( h_x \) for condensation is determined from the definition

\[
\delta(x) = \left[ \frac{4\mu(\gamma - \beta) T_x - T_w x}{g(\gamma - \beta) \rho f g} \right]^{1/4}
\]  

(3.20)

Introducing \( \delta(x) \) from equation 3.20 into equation 3.21, one obtains:

\[
h_x = \frac{k_l}{\delta(x)}
\]  

(3.21)

And the local Nusselt number \( Nu_x \) is expressed as

\[
Nu_x = \frac{h_x x}{k_l} = \left[ \frac{g(\gamma - \beta) h_f g k_l^2}{4\mu(\gamma - \beta) T_x - T_w x} \right]^{1/4}
\]  

(3.22)

(3.23)

One may notice from equations (3.20-22) that the local heat transfer coefficient \( h_x \) varies with the distance as \( x^{-1/4} \). Then the average heat transfer coefficient \( h_m \) over the length \( 0 \leq x \leq L \) of the plate is:

\[
h_m = \frac{1}{L} \int_0^L h_x dx = \frac{4}{L} h_x \bigg|_{x=L}
\]  

(3.24)

Or, introducing equations (3.20-22) into equations (3.20-24), one obtains:

\[
h_m = 0.943 \left[ \frac{g(\gamma - \beta) h_f g k_l^2}{\mu(\gamma - \beta) T_x - T_w L} \right]^{1/4} \text{ W/(m}^2\cdot\text{C)}
\]  

(3.25)

The physical properties in equations (3.20-22) and (3.20-3.25), including \( h_f g \), should be evaluated at the film temperature

\[
T_f = \frac{1}{2} (T_w + T_v)
\]  

(3.26)

The additional energy needed to cool the condensate film below saturation temperature is accommodated approximately by evaluating \( h_{fg} \) at the film temperature instead of the saturation temperature.

A comparison of the average heat transfer coefficient for vertical surfaces given by equations (3.20-25) with that found by experiments shown that the measured heat transfer coefficient is about 20 percent higher than theory would suggest. Therefore, McAdams recommends that Nusselt’s equation for \( h_m \) on a vertical surface is multiplied by a factor of 1.2; hence equations (3.20-25) should be replaced by

\[
h_m = 1.13 \left[ \frac{g(\gamma - \beta) h_f g k_l^2}{\mu(\gamma - \beta) T_x - T_w L} \right]^{1/4}
\]  

(3.27)

Nota. Se retiraste isto do Ozisik tens de lhe fazer referencia. O texto nao pode estar literalmente copiado do livro e as Figuras nao podem ser exactamente iguais.
3.4 Cooling configurations using phase change

Several techniques make use of materials phase change to cool down electronic components. Most of them use the boiling of a liquid to achieve higher heat fluxes. Some of these strategies include pool boiling [45, 46, 47, 14, 12, 15, 48], micro-channels [17, 19, 49, 16, 18], jet or spray impingement [20, 8, 13, 22, 50, 51], as revised in Chapter 2. Each of these techniques has different advantages and drawbacks, which will be briefly reviewed in this sub-section.

Pool boiling, is a direct immersion liquid cooling technique, since there are no physical walls separating the heated surface from the liquid coolant. This form of cooling offers the opportunity to remove heat directly from the heated surface, in this case the CPU with no intervening thermal conduction resistance, other than that between the CPU and the heat spreader surface in contact with the liquid. Interest in pool boiling as a method for cooling integrated circuit chips may be traced back as early as the 1960s. Pool boiling offers a high heat transfer coefficient which reduces the temperature rise of the chip surface above the liquid coolant temperature. The selection of a liquid for Pool boiling cannot be made on the basis of heat transfer characteristics alone. Chemical compatibility of the coolant with the electronic chips and other packaging materials exposed to the liquid must be a primary consideration.

The term ‘micro’ is applied to devices having hydraulic diameters of ten to several hundred micrometers. In many practical cases, the small flow rate within micro-channels produces laminar flow resulting in a heat transfer coefficient inversely proportional to the hydraulic diameter. In other words, the smaller the channel, the higher the heat transfer coefficient. Unfortunately, the pressure drop increases with the inverse of the second power of the channel width, keeping the mass flow constant, and limiting ongoing miniaturization in practice. Mudawar [21] reviewed high-heat-flux thermal management schemes, including ultra-high-heat-fluxes in the range of $1000 - 100,000 \text{ W/cm}^2$. In recent years spray cooling has received increasing attention as a means of supporting higher heat flux in electronic cooling applications. Spray cooling breaks up the liquid into fine droplets that impinge individually on the heated wall. Cooling of the surface is achieved through a combination of thermal conduction through the liquid in contact with the surface and evaporation at the liquid-vapor interface. The droplet impingement both enhances the spatial uniformity of heat removal and delays the liquid separation on the wall during vigorous boiling. Spray cooling has gained a foothold in the military sector providing for improved thermal management, dense system packaging, and reduced weight.

Reparei pelo ingles e pelo vocabulario que esta parte do texto foi retirada de algum lado....altera o texto por palavras tuas...nao podes copiar directamente excertos tão grandes de um texto.

Pool boiling is not the technique which offers the highest heat transfer coefficients, but it was chosen as its the simple hardware requirements and the almost absence of pumping auxiliary components provide great advantages over other much more complex configurations. At this stage it is worth mentioning that not all the liquids can be used for cooling. For instance, although it has high values of thermal properties and particularly high values of the latent heat of vaporization, liquids like
water are dangerous to use, even in indirect cooling techniques, due to the risk of leakage. Hence, the working fluids must be dielectric. Additionally, it is recommended that the saturation temperature of the working fluid at ambient pressure (the temperature at which phase change begins) is as close as possible to the working temperature of the system to cool.
Chapter 4

Peltier Cells

Given that the achievement of the objectives of the present work requires deep understanding on the Peltier cells working principles and main characteristics, this chapter addresses the fundamental theoretical concepts governing the working principles of the Peltier cells, as well as benefits and drawbacks of using them for several purposes (including cooling systems). Section 4.1 provides a brief historical introduction to the Peltier cells. Section 4.2 will discuss some of benefits and drawbacks of using the Peltier cells in various relevant applications. Section 4.3 explains the thermoelectric effect in more detail and section 4.4 introduces the formulation that describes its behaviour. Finally, Section 4.5 explains the main characteristics and procedures that must be considered to select the appropriate Peltier cell for the required application.
4.1 Introduction

Peltier thermoelectric cells (TEC) are solid-state devices that create an electrical voltage from a temperature gradient (Seebeck effect) or convert an electrical voltage into a temperature gradient (Peltier effect).

Baltic German physicist Thomas Johann Seebeck, in 1821, was the first to found that in a loop made of two dissimilar conductors, with junctions at different temperatures would deflect a compass magnet [52]. Seebeck initially thought that this temperature gradient caused an induced magnetism and this was related to Earth’s magnetic field [53]. Quickly he realized that an electromotive force (emf) and consequently, by Ampère’s Law, an electric current is generated due to the temperature difference. This is known as the Seebeck effect and it is widely used to measure temperature with great sensitivity accuracy in thermocouples.

Later in 1834, French physicist Jean Charles Athanase Peltier discovered that when an electrical current is made to flow between two dissimilar conductors, one junction is cooled and the other is heated, thus creating a temperature gradient. In 1838, Heinrich Lenz showed that depending on the direction of the current flowing, heat could be removed from a junction to turn water into ice, or reversely could be added to the junction to melt ice [53].

Twenty years later (1854), British physicist William Thomson (Lord Kelvin) issued a comprehensive explanation of the Seebeck and Peltier effects and described their interrelationship [53]. The Seebeck and Peltier coefficients are related, being the Peltier coefficient simply equal to the Seebeck coefficient multiplied by the absolute temperature. This thermodynamic derivation led Thomson to predict a third thermoelectric effect, now known as Thomson effect, which occurs when heat is absorbed or produced while an electric current passes through a circuit composed of a single material that has a temperature difference along its length. If a copper wire carrying a steady electric current is subjected to external heating at a short section while the rest remains cooled, heat is absorbed from the copper as the conventional current approaches the hot point, and heat is transferred to the copper just beyond the hot point.

4.2 Peltier cells in various applications: advantages and drawbacks

Peltier cells provide numerous solutions to many applications and in several cases they are the only reliable solution [54]. Working on a thermoelectric basis, Peltier cells are widely used as heat pumps or coolers. They are often applied as thermal energy sensors, in aeronautics and space, in small-scale refrigeration [25].

While one cannot select a cooling method to be the best, given the numerous variables that
must be considered in heat transfer problems, Peltier cells have several characteristics that make them a very interesting solution to approach [30]. Some advantages of using Peltier cells are:

- No moving parts: so maintenance is required less frequently.
- Small size and weight: they are much smaller than comparable mechanical systems and come in a wide variety of sizes and forms to comply with strict requirements [31].
- Ability to cool below ambient temperature: unlike air cooling, Peltier cells have the ability to cool the temperature below the ambient value.
- Ability to either heat or cool with the same module: as demonstrated by Lenz, to exchange between heating or cooling, one just has to reverse the polarity of the applied current.
- Precise temperature control: with an appropriate control system, Peltier cells are able to control the temperature with an accuracy of +/- 0.1°C [55].
- High reliability: due to the solid-state construction with mean time between failures (MTBF) exceeding 100,000 hours [55].
- Quiet operation: unlike air cooling they produce no noise.
- Operation in any orientation: they can operate in any direction and in zero gravity environments.
- Spot cooling (e.g. for electronic circuits): with Peltier cells allow cooling a specific region of the circuit, and thus not wasting energy cooling unnecessary components.
- Ability to generate electric power: when temperature gradient is applied, it is possible to generate current.
- Environmentally friendly: conventional refrigeration systems often use chlorofluorocarbons that can be harmful to the environment. Peltier cells do not use or generate gases of any kind.

However, there also have some disadvantages:

- Able to dissipate limited amounts of heat flux.
- Condensation is another potential dangerous problem, occurring if components are cooled too much
- Not as efficient, in terms of the Coefficient of Performance (C.O.P), as vapour-compression systems (The C.O.P is further defined in section 4.5).

### 4.3 Thermoelectric Effect

The thermoelectric effect is much larger at metal-semiconductor junction than in a junction between two metals. In the world of thermoelectric technology, semiconductors (usually Bismuth-Telluride) are the material of choice for producing the Peltier effect. These semiconductors are used because designers can easily optimize the pumping of heat by controlling the type of charge carrier employed within the conductor. A Peltier cell in its simplest form can be composed of a single n-type
pellet [56] which is connected to an electrically-conductive wire on each end (Figure 4.1).

![Figure 4.1 – Single N-type pellet](image1)

As shown in Figure 4.1, the heat will be pumped in the direction of the charge flow. Actually the heat is transferred by the carrier charges. In this N-type semiconductor the electrons will be the charge carriers within the molecular structure. When a DC voltage source is applied, the electrons will be repelled by the negative pole of the source and attracted to the positive pole as shown in the figure. With the electrons flowing through the n-type semiconductor from bottom to top, the heat is absorbed in the bottom and actively pumped to the top junction. P-type pellets (Figure 4.2) are also widely used in thermoelectric industry.

![Figure 4.2 – Single P-type pellet](image2)

P-type pellets are manufactured so that the charge carriers in the semiconductors are positive (known as “holes”). These are places where the electrons can easily fit when a voltage is applied, thus enhancing the electrical conductivity of the material. Positive charge carriers are repelled by the
positive pole of the voltage source and attracted to the negative pole, so that “hole” current flows in an opposite direction to that of the electron flow and so the heat is moved from top to bottom.

This contrast in heat pumping between N-type and P-type pellets is very important in the design of Peltier cells. Although it is possible to make a simple thermoelectric cooler with a single semiconductor pellet, we are unable to pump a considerable amount of heat through it. Hence, Peltier cells are not made solely by one N-type or one P-type pellets, but instead it is composed of several N-type and P-type pellets. In order to pump larger amount of heat, the most intuitive though is to connect the pellets in parallel, both electrically and thermally, as shown in Figure 4.3.

![Figure 4.3 – Multiple P-type pellets connected in parallel](image)

However, this is a very unpractical approach since the typical thermoelectric semiconductor pellet is rated for only a very small voltage while it can draw a considerable amount of current. For example, a single pellet in an ordinary thermoelectric cell may draw five amps or more with only 60mV applied; if wired in parallel in a typical 254-pellet configuration, the device would draw over 1270A with the application of only 60mV. As easily seen, this is an unpractical approach. So, the only realistic solution is to make the electrical connection of the pellets in series, while keep them thermally in parallel. Here the idea could be to connect them in a zigzag fashion from pellet to pellet to achieve a series circuit. In theory this is a good idea, however, in reality the interconnections between the pellets introduce thermal shorting that significantly compromises the performance of the device.

Fortunately, there is one final approach that serves the intended purpose which is to arrange n and p-type pellets in a couple and forming a junction between them with a platted copper tab. With this configuration it is possible to pump all the heat in the same direction.

As shown in Figure 4.4, with the bottom of the p-type pellet connected to the positive pole of the voltage source we are able to reverse the direction of the charge carriers and with this we are able to pump all the heat in the same direction. In this configuration the electrons in the n-type pellet are repelled by the negative pole of the source and flow into the copper plate. When they reach the p-type material they simply flow through the holes and into the positive pole of the source. The “holes” from the p-type pellet are repelled by the positive pole and drawn into the negative pole of the supply. This way, the heat and the charge carriers are both flowing into the same direction through the pellets (bottom to top). Using this configuration it is possible to arrange multiple pellets with this configuration
and pump a considerable amount of heat. Furthermore, with the electrical wiring in series this configuration is suitable for DC power supplies. Thus the most common thermoelectric devices nowadays, connecting 254 alternating n and p-type pellets, can run from 12 to 16VDC supply and draw 4 to 5A, rather than 1270A at 60mV, for example (Figure 4.5).

![Figure 4.4 – Single N-P-type pellet](image)

![Figure 4.5 – Multiple N-P-type pellets](image)

When manufacturing devices with multiple pellet arrays, we must have the means to mechanically hold everything together. The industry standard solution is to use thin ceramic substrates mounted on both sides of the conductive tabs (Figure 4.6). Besides providing protection against mechanical external forces, the ceramic substrates also act as the thermal interface between the Peltier cell and its surrounding. These have become the industry standard because they represent the best compromise between mechanical strength, electrical resistivity, thermal conductivity and cost.

![Figure 4.6 – Typical Configuration of a Peltier device](image)
4.4 Thermoelectric Cooling

With the configuration shown in Figure 4.5, the thermoelectric power of these devices is large enough to be of practical interest for electronic cooling, particularly where the absence moving parts and the strong restriction to use small size components are issues of vital importance.

![Diagram of a thermoelectric cooler](image)

**Figure 4.7 – Current Flowing through N-P junction**

The current I in Figure 4.7 pumps heat from bottom (cold) junction to the top (hot) junction, cooling it by $\Delta T$ below the temperature of the hot junction ($\Delta T = T_h - T_c$). The cooling effect of Peltier cells is reduced by Joule effect and thermal conductance of the material used. The heat removed at the cold junction is expressed as [26, 55, 30, 31, 27]:

$$\dot{Q}_c = 2N[s I T_c - \frac{1}{2} I^2 \rho \frac{s}{\sigma} - k G \Delta T]$$ (4.1)

or

$$\dot{Q}_c = 2N[P I - \frac{1}{2} I^2 \rho \frac{s}{\sigma} - k G \Delta T]$$ (4.2)

Where, $\dot{Q}_c$ is the heat removed from the cold junction,

$s$ is the Seebeck Coefficient,

$\rho$ is the electrical conductivity of the semiconductor,

$k$ is the thermal conductivity,

$N$ is number of pairs of thermoelectric elements

$G$ is area/length of thermoelectric cell,

$P$ is the Peltier Coefficient ($P = S T_c$).

The factor $\frac{1}{2}$ of Joule effect comes from the equation of heat-transport. The equation 4.1 is easily explained by Figure 4.8. Also there is the thermal conductance where heat naturally moves to colder regions when there is a temperature gradient. For simplicity, one can define [27]:

---

31
where \( s \), \( \rho \) and \( k \) are physical properties of the thermoelectric materials and \( S_m \), \( R_m \) and \( K_m \) are physical characteristics of Peltier cell as devices, i.e., the latter depend on the geometry, dimensions and the arrangement of the pairs of thermoelectric elements. With equations 4.3, 4.4 and 4.5, equations 4.1 and 4.2 can be rewritten as

\[
\dot{Q}_c = S_m I T_c - \frac{1}{2} I^2 R_m - K_m \Delta T \tag{4.6}
\]

and

\[
\dot{Q}_c = p_m I - \frac{1}{2} I^2 R_m - K_m \Delta T \tag{4.7}
\]

Similar equations can be used for the heat power released at the hot side junction, where the Joule effect adds heat to the equation:

\[
\dot{Q}_h = S_m I T_h + \frac{1}{2} I^2 R_m - K_m \Delta T \tag{4.8}
\]

Figure 4.8 – Heat flow through a Peltier cell

The Joule effect is simply the result of the electrical power supplied to the system which is the product of the current and voltage. These magnitudes are not related by a constant resistor value like in other electronic circuits, since for a given current, the required voltage depends on the temperature.
of the system, given that \( \rho \) depends on the temperature.

\[
P = VI \tag{4.9}
\]

So the power balance equation will be given by:

\[
P = \dot{Q}_h - \dot{Q}_c \tag{4.10}
\]

\[
VI = S_m I T_h + \frac{1}{2} I^2 R_m - K_m \Delta T - S_m I T_c + \frac{1}{2} I^2 R + K_m \Delta T \tag{4.11}
\]

\[
VI = R_m I^2 + S_m (T_h - T_c) I \tag{4.12}
\]

Therefore the simplified equation for the voltage across the Peltier cells is:

\[
V = R_m I + S_m \Delta T \tag{4.13}
\]

This equation is very important when estimating \( R_m \) and \( S_m \) from the performance curves of Peltier cells manufacturers. Usually, a certain \( \Delta T \) is obtained for a given voltage and current, for different values of \( \dot{Q}_c \). Equation 4.13 contains just two parameters that can be easily estimated knowing the \( V \), \( I \) and \( \Delta T \). After obtaining \( R_m \) and \( S_m \), other physical properties (\( s \), \( \rho \) and \( k \)) can be derived directly.

In datasheet curves, only two extreme situations are represented, \( \Delta T = 0 \) and \( \dot{Q}_c = 0 \), since all other are in between. These situations are presented as the maximum achievable \( \Delta T \) occurs when no heat is being transported. Reversely, the maximum amount of heat (\( \dot{Q}_c \)) is absorbed at \( \Delta T = 0 \), i.e., \( T_h = T_c \). Therefore assuming \( \Delta T = 0 \), equation 4.13 becomes \( V = R_m I \), therefore

\[
R_m = \frac{V}{I} \tag{4.14}
\]

Knowing the maximum amount of heat pumped \( \dot{Q}_c \), which usually is one of the key parameters given by the manufacturers, it is possible to apply to equation 4.6

\[
\dot{Q}_c = S_m I T_c - \frac{1}{2} R_m I^2 \tag{4.15}
\]

And obtain the value \( S_m \) from

\[
S_m = \frac{\dot{Q}_c - \frac{1}{2} R_m I^2}{I T_c} \tag{4.16}
\]

Finally, the last characteristic of the module is parameter \( K_m \), related to thermal conductivity. In this case, assuming \( \dot{Q}_c = 0 \), equation 4.6 becomes

\[
K_m = \frac{S_m I T_c - \frac{1}{2} R_m I^2}{\Delta T} \tag{4.17}
\]
4.5 Selection of the Peltier cells: Relevant characteristics and procedures

There are several characteristics that one must take into account when selecting the appropriate Peltier cell to use. The key parameters usually given in a datasheet are $\dot{Q}_{c_{\text{max}}}$, $\Delta T_{\text{max}}$, $V_{\text{max}}$ and $I_{\text{max}}$. The most relevant is the amount of heat ($\dot{Q}_{c_{\text{max}}}$) the Peltier cell can remove. One must ensure that $\dot{Q}_{c_{\text{max}}}$ is higher than the maximum amount of heat $\dot{Q}_c$ generated by the system to be cooled. The next step is to determine the current ($I$) required to remove $\dot{Q}_c$ and to generate the desired $\Delta T$. By knowing the power consumed $P = VI$ to remove $\dot{Q}_c$ one can estimate the Coefficient of Performance (C.O.P.)

$$C.O.P. = \frac{\dot{Q}_c}{P}$$

(4.18)

It is not unusual to have a C.O.P. lower than one, i.e., consuming more power than the power removed. Peltier cells are inefficient in comparison to other cooling solutions, like vapour-compression systems. Their advantage is the precise control of temperature and being almost independent of the ambient temperature. However, with careful design of the system one can easily rise the C.O.P to values higher than 1.5. This can be achieved, for example, by using a Peltier device with a $\dot{Q}_{c_{\text{max}}}$ much higher than $\dot{Q}_c$. Assume two different Peltier devices, number one with $\dot{Q}_{c_{\text{max}}} = 80W$ and number 2 with $\dot{Q}_{c_{\text{max}}} = 300W$. If they are to remove a $\dot{Q}_c = 60W$, the number two will probably have a higher C.O.P. than number one. This happens because number one is much closer to its maximum potential than number two. While it is true that as one increases the current supplied to the Peltier device so increases the amount of power the Peltier device is able to remove, after a certain current the additional power gained is outweighed by the additional heating (Joule effect) generated by the device itself. Because number one is much closer to its potential, its Joule effect will be greater than number two.

Another way to increase the C.O.P. is to change the number of Peltier cells one is going to use. For example, assume a Peltier device that can remove 60W with 5A and 30W with 2.2A. For 30W the current drawn is not 2.5A because the amount of heat removed by the cell in nonlinear with the power given, i.e., they are more inefficient as they reach their potential. If one chooses to use to use 2 Peltier cells of the same model in thermodynamic parallel we are able to remove 60W with 2.2A each (4.4A total instead of 5A). This allows us to remove the same amount of heat with lower power given to the cells which results in lower Joule effect and consequently a higher C.O.P.
Chapter 5

Experimental Apparatus, Procedures and PID Controller

This chapter starts by presenting in section 5.1 the conceptual design of the system, its components and requirements. To achieve a practical system it is important to understand and characterize the Peltier cells. In this context, an additional setup had to be developed for accomplishing with this characterization and with the design of the control system, which is presented in section 5.2. This setup is already a good approximation of the final system. Finally, a preliminary configuration of the final setup for the use of the cooling system in a personal computer is proposed in section 5.3.

The characterization tests of the Peltier cells, PID controller gains and final setup were performed following well established experimental procedures, which are described in section 5.4.
5.1 Conceptual Design

The conceptual design of the system is represented in Figure 5.1. The essential components of the system are:

- 1 - CPU
- 2 - Pool
- 3 - Peltier cell
- 4+5 Dissipator+Fan (to cool the Peltier cells)
- Control system

Figure 5.1 – Conceptual design. The numbers identify each of the aforementioned essential components of the system.
Each component of the system was chosen carefully to satisfy the various requirements that the system must meet. The following paragraphs will explain the reasoning for the selection of each component and its requirements.

### 5.1.1 Central Processing Unit (CPU)

The conceptual purpose of the project in which this work inserted is to develop a cooling system for the latest generation personal computers. However, a Pentium 4 2.4B GHz was chosen to test first since there was already a prototype of the pool designed for this processor. Also, the thermal management problems observed in the Pentium 4 processors [57] are well known, so this processor can already be a test to the cooling system developed here.

### 5.1.2 Pool

In the initial prototype, the pool was designed taking into account thermodynamical requirements. The purpose of the initial design was to be the simplest possible and to demonstrate the feasibility of the cooling system. The pool was made of acrylic due to its thermal isolating properties. Some thermodynamical requirements were satisfied, although without an extensive study of the dimensions required. Given that the CPU is surrounded by other components, the minimum height of the pool was restricted to 60mm. The size of the condensation surfaces was chosen to ensure that all the fluid mass at the most demanding cooling conditions was condensed for a given \( \Delta T \) imposed by the Peltier cells.

### 5.1.3 Peltier Cell

Several characteristics must be taken into account when choosing a Peltier cell. As previously explained in section 4.5, the most relevant is the maximum amount of heat that can be removed by the device \( (\tilde{Q}_c) \). One must ensure that the maximum possible heat generated \( (\tilde{q}_c) \) by the system is lower than \( \tilde{Q}_{c,\text{max}} \). Two other relevant characteristics are the energy consumed by the device and the internal heat generated by its functioning (Joule effect). When choosing a Peltier cell, one must take into account how to supply the energy required for the device to remove a determined amount of heat. There are several ways to supply the energy required by the device: pulse-width modulation (PWM), voltage source or current source. Peltier cells work on current but usually have significant enough resistance so that voltage control is possible. Running the Peltier cell with pulses is a bad choice, particularly in cooling applications: while cooling increases with increasing current, efficiency is reduced as the current increases. The cooling effect is proportional to the current, but the Joule effect is proportional to the square of the current \( (R I^2) \). Above a determined current, the Joule effect outweighs the additional cooling power obtained by the higher current. Therefore, to PWM a Peltier device between 0 and the maximum cooling current is not desired. By PWM a Peltier device we would be alternating between off and a state of the Peltier cell which is extremely inefficient because at the maximum cooling current the Joule effect clearly outweighs the heat removed. Finally, if thermally
cycling occurs as a part of the control process, the mechanical wear will strongly reduce the lifespan of the device.

Since Peltier devices work on current, a current control approach is preferred to a voltage control. Section 5.2.5 will provide an additional reason why it was chosen to control the Peltier device by imposing the current.

The Joule effect is relevant when choosing a Peltier device because, if the device chosen has a $\dot{Q}_{c_{\text{max}}}$ very close to the heat being removed, the device will be running close to its maximum potential and Joule effect will increase significantly, resulting in a very poor C.O.P. (as defined in Section 4.5, eq. 4.18) and creating several difficulties to dissipate the total heat of the system (as the amount of heat to be removed to cool the device is added to a significant amount of heat that is dissipated in the cell by Joule effect). This is a very important factor to be taken into account since, if the characteristics and working conditions of the cells are not carefully chosen, the Joule effect may imply the use of much powerful additional systems to cool the cells, which would overcome the advantage of using the Peltier cells, thus jeopardizing the implementation of the current cooling configuration.

The Peltier device used in the following setups is the MCPF-127-14-11-E, depicted in Figure 5.2, manufactured by Multicomp. Its most relevant characteristics are presented in Table 5.1. However, this Peltier cell was our second choice. The first choice was the TEC1-26316 manufactured by Hebei which has $\dot{Q}_{c_{\text{max}}} = 300\text{W}$ and $\Delta T_{\text{max}} = 66^\circ\text{C}$. This was first selected taking in mind the Thermal Design Power (TDP) of the latest generation personal computer which is higher than 150W. This would give us a greater flexibility and a better C.O.P. as explained in section 4.5. After some preliminary tests, we concluded that a very efficient cooling of the Peltier cell was required to remove the significant additional amount of thermal energy which was generated by Joule effect. Another problem raise in the use of the TEC1-26316 cells was the high current drawn ($I_{\text{max}} = 16\text{A}$), which is higher than most power supplies available to us could output. Instead, MCPF-127-14-11-E was selected because its $\dot{Q}_{c_{\text{max}}} = 79\text{W}$ is higher than the TDP of the CPU we pretended to test (59W), which could still assurance us flexibility. Its maximum current was 8.5A which is a much more reasonable and safe value to work with, particularly when compared to the 16A required by the TEC1-
As explained in section 4.5, the use of two Peltier devices instead of one allows us to reduce the Joule effect of the system and hence improving the C.O.P.. One of the requirements of the condensation system is to generate a $\Delta T$ around 8-10°C on the top of the pool so that condensation of HFE-7000 is ensured. This $\Delta T$ is a typical reference value so that condensation occurs. According to preliminary results from the characterization of the Peltier cells, while removing 30W with a current of 6A, the $T_c$ of the Peltier device was at 30°C. Hence, to remove the 59W of the Pentium 4, two Peltier cells would be needed. Only by using two Peltier cells one could remove the 59W released by the CPU and create a temperature difference large enough so that condensation could occur.

Table 5.1 - Multicomp MCPF-127-14-11-E Characteristics

<table>
<thead>
<tr>
<th>Manufacturer Reference</th>
<th>MCPF-127-14-11-E</th>
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<tbody>
<tr>
<td>Power Rating</td>
<td>79W</td>
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<tr>
<td>Internal Resistance</td>
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<tr>
<td>Current Max at $\Delta T_{max}$</td>
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<td>Voltage Max at $\Delta T_{max}$</td>
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<tr>
<td>Solder Melting Point</td>
<td>232°C</td>
</tr>
</tbody>
</table>

5.1.4 Zalman CNPS7500-AlCu LED Fan

The fan used was the CNPS7500-AlCu LED, depicted in Figure 5.3, manufactured by Zalman. The purpose of the fan is simply to dissipate the additional amount of heat which is generated by Joule effect in the Peltier cell. This fan was chosen because it presented good performance/price ratio. The base material is composed by pure copper and pure aluminium. Its dimensions are 121mm (Length) x 121mm (Width) x 67mm (Height) with a weight of 500g. The dissipation area is 3500cm². The fan operates at 2,550rpm (34.5dBA) if connected directly to the power supply without the use of Fan Speed Controller FAN MATE2.
The proper design a controlled condensation system, using Peltier cells requires an accurate characterization of the cells, which is vital to confirm the selection of the cells as well as to obtain already several characteristic parameters, such as the internal resistance $R_m$, the Seebeck coefficient $S_m$, and Thermal Conductance $K_m$. The dynamic response of the cell in time is also important, as further discussed in the results. These properties must be known a priori, so these tests cannot be performed in the final setup.

Confirming the characteristics of the selected cells on real working conditions is also a crucial step, as the data provided in the datasheet are often obtained at testing conditions quite different from ours. Actually, the temperature, which is a key parameter, is significantly different since in datasheets, the performance curves are usually given for a fixed temperature ($T_h$) of the hot surface, which is very difficult to obtain in a real application.

In this context, an additional setup was developed. This setup is a simplified version of the conceptual design, in which the CPU was replaced by a resistance regulated by a potentiometer. This was done so that one could impose a well-defined heat power. Also, the pool was omitted from this setup, since the main purpose is to characterize the Peltier device itself and not its performance under the configuration for which the cells are used for liquid condensation. All tests were performed with a single Peltier device cooled by one fan.

The setup used is represented in Figure 5.4, in which the main components are identified by numbers. As aforementioned, the CPU was replaced in this setup by a resistance of 823 $\Omega$ (1 in Figure 5.4) regulated by a potentiometer (2 in Figure 5.4). The potentiometer was connected directly to the power grid, so alternating current was flowing through the resistance. In this way, one could determine at any given time the $\dot{Q}_c$ removed by the Peltier cell, which equals the power imposed to the resistance. This resistance is thermally isolated with natural rubber. The calibration of the potentiometer was made by measuring the voltage and current flowing at the entrance of the resistance with the use of two different multimeters. The multimeter Range RE-68, identified by the
number 3, measured the alternating current and the multimeter Xindar DB600.031, identified by the number 4, measured the alternating voltage. Figure 5.5 shows the potentiometer used. The multimeter RE-68 has an accuracy of +0.5% for DCV, +0.8% for ACV, +1.2% for DCA and +1.2% for ACA.

Figure 5.4 – Setup developed to characterize the Peltier cells

Figure 5.5 – Potentiometer and Thermocouples placement in the resistance

This resistance is inserted in a stainless steel block over which the Peltier cell is placed, being in contact with the cold surface of the Peltier cell and the hot surface is in contact with the fan. The entire block is isolated with rubber to assure that the heat flux is mainly directed upwards and to
minimize the heat losses to the environment. Three type K thermocouples are inserted to acquire the temperature of the steel surface, the temperature of the cold surface (number 2 in Figure 5.5) and the temperature of the hot surface (number 1 in Figure 5.5) of the Peltier cell. The thermocouples are positioned at 1mm below and above the cold and hot surftaces of the Peltier cell, respectively. The third thermocouple (number 3 in Figure 5.5) is placed 5mm below the one measuring the cold surface.

The characteristics of the Peltier cells that were used here were described in section 5.1.3. To have a controlled condensation system, one must be able to remotely control the amount of current given to the cells, by the power supply. Following this, several options were taken into consideration, namely:

- Power supply with GPIB interface
- Power supply remotely controllable by a voltage/resistance reference
- Modified Computer Power supply
- Transformer design

The easiest solution to implement was the power supply with GPIB interface. However, these power supplies are usually expensive in comparison to the other solutions and there was not any of power supply available with the adequate characteristics, which met the maximum current of 8.5A requirement.

The second option consisted in using an analog power supply remotely controllable by a voltage/resistance reference. This option was easy to implement, since there was a power supply available which met the requirements. However, one would have to choose a suitable device that would generate the voltage/resistance reference.

Given that the purpose of the project in which the present thesis is included is to create a commercial product, these two options were not commercially viable. Another option considered was to modify a computer power supply to draw the current output required. However, we do not want to generate a fixed value, so considerable study of the current computer power supplies was needed and additional electrical circuits were required, whose complexity was out of the scope of the present work. The final option considered was to develop from scratch a transformer specific for this Peltier device. This would be the ideal solution and the most appealing from the commercial perspective. However, after considerable counseling we concluded that it was not viable as the development was also significantly complex and time consuming, being, once again out of the main objectives of the present work.

After considering the benefits and drawbacks of each solution, in addition to the fact that by that time it was not yet demonstrated that the cooling system proposed was thermodynamically viable to be worth a considerable effort developing a specific power supply, it was decided to use an analog power supply remotely controllable by a voltage/resistance reference. This was the ideal solution fulfilling all the requirements. In addition, from all the solutions which were possible to implement within the time window of this project, this is also the most appealing from the commercial perspective.
The power supply available was the Hewlett Packard 6274B DC Power Supply (5 in Figure 5.4). Details of front and back panels, showing the connections to use for our specific application are given in Figure 5.6. The output of this power supply is 0-60V at 0-15A. It can be either operated in constant voltage or constant current. Optional operating modes are: remote voltage sensing, remote programming, auto-parallel operation, auto-series operation and auto-tracking operation. The operating mode of interest in this work is remote programming. In remote programming, the output voltage or current can be remotely controlled by connecting an external resistor or applying an external voltage to rear panel terminals. The programming coefficients for each solution are presented in Table 5.2. Considering that, as mentioned earlier, the Peltier devices should preferably be used in constant current and that the coefficient for constant voltage output with a voltage input was unitary, which would require another power supply to control, only two of the four options were viable. The option chosen was constant current output controlled by a voltage input because the values of input were more reasonable and easier to implement. The device chosen to create the voltage input was the microcontroller Arduino Due.

Table 5.2 - Remote programming coefficients

<table>
<thead>
<tr>
<th>Constant Voltage Output, Resistance Input</th>
<th>200Ω/V</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant Voltage Output, Voltage Input</td>
<td>1V/V</td>
</tr>
<tr>
<td>Constant Current Output, Resistance Input</td>
<td>67Ω/A</td>
</tr>
<tr>
<td>Constant Current Output, Voltage Input</td>
<td>33.3mV/A</td>
</tr>
</tbody>
</table>

Several reasons were taken into consideration when choosing the use of an Arduino Due (Figure 5.7):

- It allows creating a voltage reference up to 3.3V by PWM or through the use of the incorporated 12 bits Digital-Analog Converter.
- It also allows incorporating the PID controller made in software used to control the Peltier device, which will be explained in section 5.3.
- Readings from the thermocouples used to acquire the temperature of both surfaces of the Peltier device could easily be integrated with the Arduino.
Furthermore, since the minimum interval between readings used was 1s, the Clock Speed of 84MHz allowed us to implement thousands of instructions between each reading. The 512KB of flash memory for code were more than enough. Also, there is a lot of documentation about numerous applications using Arduino as microcontroller making it easier to use.

The Arduino Due contains a 12bit Digital-Analog Converter (DAC) which allows creating a voltage reference. Later, one realized that the DAC only allows us to create an analog voltage between 1/6 (0.55V) and 5/6 (2.75V) of the input voltage (3.3V) of the Arduino Due, surpassing the limit of the HP 6274B which was 500mV \(\frac{3.3\text{mV}}{5} \times 15A = 495\text{mA}\). Hence, PWM was the method chosen to generate the voltage reference needed to remotely control the HP 6275B between 0-500mV. Having a 12bit PWM output instead of the 8bit PWM output of Arduino Uno, allows a better accuracy when generating a voltage reference.

Finally, the Arduino is responsible for reading the temperature and accordingly act on the PID controller and generates a voltage reference that will results in a higher/lower current to the Peltier cells. This way, the condensation system is independent of the system to be cooled. In this work, the application chosen was the cooling system of a personal computer, but the cooling system with the Peltier cells, with the PID controller s designed independently of the system to cool and can be easily adjusted to other applications.

![Figure 5.7 – Arduino Due](image)

Maxim MAX31855, three are mounted on the breadboard in Figure 5.7, was used for the integration of the thermocouples readings with Arduino. The Maxim Integrated MAX31855 is a sophisticated thermocouple-to-digital converter with a built-in 14-bit analog-to-digital converter (ADC).
The device also contains cold-junction compensation sensing and correction, a digital controller, an SPI-compatible (Serial Peripheral Interface) interface, and associated control logic. The device is designed to work in conjunction with an external microcontroller in thermostatic, process-control, or monitoring applications.

This converter resolves temperature to 0.25°C, allows reading as high as 1800°C and as low as -270°C, and exhibits thermocouple accuracy of +2°C for temperature ranging from -200°C to 700°C for K-type thermocouples. Several specifications are presented in Table 5.3. The pin configuration of the MAX31855 is represented in Figure 5.8 and Table 5.4. In this setup were used three integrated circuits to get the reading of the three thermocouples used. As referenced in the product datasheet, if one is using multiple MAX31855, all pins can be shared in the microcontroller except CJC.

Table 5.3 - MAX31855 Specifications

<table>
<thead>
<tr>
<th>Specification</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Supply Voltage Range</td>
<td>-0.3V to 4.0V</td>
</tr>
<tr>
<td>Operating Temperature Range</td>
<td>-40°C to 125°C</td>
</tr>
<tr>
<td>Junction Temperature</td>
<td>150°C</td>
</tr>
<tr>
<td>Thermocouple Gain and Offset Error</td>
<td>+2°C</td>
</tr>
<tr>
<td>Thermocouple Temperature Data Resolution</td>
<td>0.25°C</td>
</tr>
<tr>
<td>Internal Cold-Junction Temperature Error</td>
<td>+2°C</td>
</tr>
<tr>
<td>Cold-Junction Temperature Data Resolution</td>
<td>0.0625</td>
</tr>
<tr>
<td>Temperature Conversion Time (Temperature, Cold Junction, Fault Detection)</td>
<td>70ms</td>
</tr>
</tbody>
</table>
Table 5.4 - MAX31855 Pin Description

<table>
<thead>
<tr>
<th>PIN</th>
<th>Name</th>
<th>Function</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>GND</td>
<td>Ground</td>
</tr>
<tr>
<td>2</td>
<td>T-</td>
<td>Thermocouple Input. Do not connect to ground</td>
</tr>
<tr>
<td>3</td>
<td>T+</td>
<td>Thermocouple Input</td>
</tr>
<tr>
<td>4</td>
<td>$V_{cc}$</td>
<td>Power-Supply Voltage</td>
</tr>
<tr>
<td>5</td>
<td>$SCK$</td>
<td>Serial-Clock Input</td>
</tr>
<tr>
<td>6</td>
<td>$\overline{CS}$</td>
<td>Active-Low Chip Select. Set \overline{CS} low to enable the serial interface.</td>
</tr>
<tr>
<td>7</td>
<td>$SO$</td>
<td>Serial-Data Output</td>
</tr>
<tr>
<td>8</td>
<td>$DNC$</td>
<td>Do Not Connect.</td>
</tr>
</tbody>
</table>

5.2 Final Setup

To test the feasibility of the condensation system implemented, a preliminary cooling setup was developed, which was tested for several conditions in a working personal computer. In this setup, the CPU (number 1) used is a Pentium 4 2.40B GHz. As mentioned earlier, since the cooling system is independent of the CPU used, this can be replaced for a more powerful one in the future tests, with
minor modifications. The geometry of the pool was redesigned for the implementation of two Peltier cells to optimise the condensation process. A complete overall picture of this setup is shown in Figure 5.9. The number 2 is the redesigned pool to optimize the condensation system. Number 3 are the fans used. The Peltier cell can be seen in the figure because they are between the pool and the fans. Number 4 is the Arduino Due, number 5 the breadboard with the three MAX31855 and finally number 7 with the HP 6274B.

The CPU used in this setup is the Intel Pentium 4 2.4B GHz, with 512KB of L2 Cache and 533MHz Front-Side Bus Speed. Its lithography is 130nm and maximum thermal design power is 59.8W. The package size is 35mm x 35mm and the socket supported is the PPGA478.

5.2.1 Final Pool

To maximize the condensation area and to take the most out of the Peltier cells performance without taking them to extreme working conditions, the pool configuration chosen to test the final set-up considered the use of 2 Peltier cells mounted vertically on each side wall of the pool.

The dimensioning, fabrication and assembly of the pool have been perfomed taking into account thermodynamic and geometrical constraints related with the particular application. Extreme attention had to be paid in how to fix the assembly pool/fans/peltier cells and how to proper positioning it on top of the CPU taking into account the presence of the others components of the motherboard. In
Figure 5.10 and Figure 5.11 are reported the global view and the typical dimensions of the assembly pool/fans/peltier cells.

The dielectric liquid (HFE 7000) contained inside the pool is directly in contact with the CPU and starts to boil as the device starts to work. Then it condenses mostly on the vertical aluminum walls that are constantly cooled by mean of the Peltier coolers. The fans are then used to cool the Peltier cells during the application. The aluminum walls are in contact in the internal side with the condensing vapor for an area of 40x115 mm^2. To avoid external environmental influence the Aluminum walls are insulated all around the Peltier cells. In Figure 5.12 we report a detail of the coupling Fan/Peltier/Insulation/Aluminum wall.

Figure 5.10 – Dimensions of the final pool

Figure 5.11 – Dimensions of the final pool
The amount of fluid that could be contained in the pool has been evaluated taking into account the fact that to condensate is required a specific cooled area. In this case only the aluminum slabs cooled by the cells has been considered as active condensation area, thus by mean of the theory of film condensation of vertical wall the following procedure to evaluate the liquid level has been followed.

1- The thermal load to be removed is:

\[ Q_{\text{cpu}}[W] = 60 \]

2- By previous experiment is has been revealed that the two Peltier cells could remove 30 W of heat power meanwhile keeping the wall temperature \( T_{\text{wall}} = 26 - 28 \, ^\circ\text{C} \). Thus since for HFE 7000 the \( T_{\text{sat}} = 34 \, ^\circ\text{C} \) we can have a \( T_{\text{sat}} - T_{\text{wall}} = 8 - 6 \, ^\circ\text{C} \) to condense the vapor generated.

3- Considering film condensation on vertical walls we then obtain the value of average heat transfer coefficient according to the Nusselt equation taking into account the thermo physical properties of the fluid at \( T = (T_{\text{sat}} - T_{\text{wall}})/2 \).

\[
h_m \left[ \frac{W}{m^2 \cdot K} \right] = 1.13 \left[ \frac{g \rho_l (\rho_l - \rho_v) h_f g k_f^2}{\mu_l (T_{\text{sat}} - T_{\text{wall}}) L_{\text{cond}}} \right]^{1/2}
\]

4- In the formulation the parameter \( L_{\text{cond}} \) is the vertical length of the condensing area thus imposing the heat to be removed and the \( T_{\text{sat}} - T_{\text{wall}} \) available one can find the needed Area to condense as:

\[
A[m^2] = \frac{Q_{\text{cpu}}}{h_m(T_{\text{sat}} - T_{\text{wall}})}
\]

And \( L_{\text{cond}} \) as:

\[
L_{\text{cond}}[m] = \frac{A}{S}
\]

In which \( S \) is the horizontal dimension of the aluminum wall (40 mm)
5. Finally the level of liquid \( (L_{\text{liquid}}) \) that can be contained in the pool resulted as:

\[
L_{\text{liquid}}[\text{mm}] = L_{\text{tot}} - L_{\text{cond}}
\]

In which \( L_{\text{tot}} \) is the total vertical extension of the aluminum wall.

5.2.2 Working fluid - HFE-7000

HFE-7000 was the fluid chosen to perform pool boiling, since it fulfills all the requirements identified in Chapter 3 (section 3.4), namely it is a dielectric fluid, which boils at 34ºC, thus its boiling point at ambient pressure assures that phase change of this liquid will occur for the typical working temperatures of the processor, thus ensuring the processor will keep working at a stable temperature. Furthermore, for the range of working temperatures, the system will operate in region III of the boiling curve between point B and C (Figure 3.3 in Chapter 3). The drawback of this fluid, which is common to most of the refrigerants is its low thermal properties and particularly the low value of the latent heat of evaporation. The most relevant thermophysical properties of HFE 7000 are depicted in Table 5.5, together with the properties of water, to provide a term of comparison.

<table>
<thead>
<tr>
<th>Property</th>
<th>Water</th>
<th>HFE7000</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tsat (°C)</td>
<td>100</td>
<td>34</td>
</tr>
<tr>
<td>Liquid density - ( \rho_l ) (kg/m³)</td>
<td>957.8</td>
<td>1374.7</td>
</tr>
<tr>
<td>Vapor density - ( \rho_v ) (kg/m³)</td>
<td>0.5956</td>
<td>4.01</td>
</tr>
<tr>
<td>Liquid dynamic viscosity - ( \mu_l ) (mN m/s²)</td>
<td>0.279</td>
<td>0.3437</td>
</tr>
<tr>
<td>Heat capacity - ( c_{pl} ) (J/kgK)</td>
<td>4217</td>
<td>1352.5</td>
</tr>
<tr>
<td>Thermal conductivity - ( k_l ) (W/mK)</td>
<td>0.68</td>
<td>0.07</td>
</tr>
<tr>
<td>Latent heat of vaporization - ( h_{fg} ) (kJ/kg)</td>
<td>2257</td>
<td>142</td>
</tr>
<tr>
<td>Liquid surface tension - ( \sigma_{lv} ) (N/m) x 10³</td>
<td>58</td>
<td>12.4</td>
</tr>
</tbody>
</table>

Nevertheless, the low saturation temperature is an advantage that must be well managed to overcome the aforementioned disadvantage. Hence, efficient control of the condensation system allowing efficient recovery is important.
5.3 PID Controller

The Proportional integral derivative (PID) controller was chosen to be implemented because without knowledge of the complete underlying process, the PID controller was chosen to assure better accuracy and reliability of the system. This is a control loop feedback mechanism that tries to minimize the error in outputs by adjusting the process control inputs [58]. The PID controller algorithm involves three separate terms: the proportional, the integral and the derivative denoted P, I and D, respectively. These terms can be interpreted as a relation between the error and time. The proportional term corresponds to the present error, the integrative term corresponds to accumulation of past errors and the derivative the prediction of future errors. Defining $u(t)$ has the controller output, the equation that describes the PID controller is:

$$u(t) = K_p e(t) + K_i \int_0^t e(\tau) \, d\tau + K_d \frac{d}{dt} e(t)$$

in which $K_p$ is the proportional term,

$K_i$ is the integrative term,

$K_d$ is the derivative term,

$e$ is the error,

$t$ is the instantaneous time,

$\tau$ is the variable of integration, that can take values between 0 and $t$.

By setting a reference value, the error is the difference between the measured value and the reference. This error is multiplied by $K_p$ which results in the proportional term of the output. In this work a discrete approach was adopted and thus the average sum of the previous and present error, multiplied by $K_i$ results in the integrative term. The derivative term is obtained from the difference between the previous and present error multiplied by $K_d$. The weight of each term in the output depends of the value given to $K_p$, $K_i$ and $K_d$. If a high value is given to $K_p$ the proportional term of the controller will be more influential than $K_i$ and $K_d$ and vice-versa.

A pseudo-code of the algorithm used is presented:

```python
define kp, ki, kd;
define reference;
current = 0.0;
error = 0.0;
previous error = 0.0;

loop()
  tc = acquire temperature;
  error = tc - reference;
  integral = (error + previous error)/2;
  derivative = (error - previous error)/2;
  previous error = error;
```
current=current + (kp*error) + (ki*integral) + (kd+derivative);
if( current < current min) current = current min;
if( current > current max) current = current max;
pwm (current);
delay (5 seconds);
}

Since it is not possible to define exactly the equations that model our system, and therefore establish the equation which describes the Peltier cell and how their physical characteristics are changing for all the tested situations, an analytical solution to obtain the gains of the PID controller was not possible.

5.4 Experimental Procedures

This section describes the experimental procedures used to accomplish the characterization of the Peltier cell, the analysis of the each term of the PID controller and the evaluation of the entire condensation system in the final cooling setup.

5.4.1 Characterization of Peltier Cells

As aforementioned, characterization of the Peltier cells is relevant, as little information about the full range of performance of a Peltier device is given in the datasheet. Usually, the parameters provided in the datasheet are: the maximum voltage and current that can be supplied to the cell, the internal resistance of the cell and the maximum temperature difference ($\Delta T_{\max}$) and power removed ($\dot{Q}_{c_{\max}}$) achievable. Furthermore, the datasheet also gives the performance curve that relates the power removed ($\dot{Q}_c$) by the Peltier device and the temperature difference between the two surfaces of the Peltier cell for several fixed values of current supplied to the device. However, this curve is only true for a fixed value of $T_h$, which is provided. For this reason, it is relevant to characterise the Peltier device for other values of $T_h$ since it is very difficult of maintain a fixed value of $T_h$ in a cooling application and this value can largely depend on the ambient temperature. Also, no information is given about the dynamic response of the Peltier device and the variation of internal resistance with temperature.

5.4.1.1 Dynamic Response

For the characterization of the dynamic response of the Peltier device, the following procedure is considered:

1. Fix a current supplied to the Peltier device.
2. Choose a known heat power created by the resistance
3. Allow the Peltier device to reach a stationary state
4. Repeat step 2 and 3 with an increased heat flux while the potentiometer has not reached its maximum value, or the temperatures are reasonable so that no damage may occur to the setup.

In this procedure, the cold surface of the Peltier cell is in contact with the resistance. The Arduino is reading the temperatures measurements every 5 seconds in both the hot and cold surface of the Peltier cell and controlling the current supplied by the HP 6274B to the Peltier cells. This interval was chosen because it was observed not significant alteration in the system that justified a smaller interval of time. The temperature measurements are made by K type thermocouples. However, these temperature measurements are converted to a digital signal by the MAX31855, which has accuracy of +2ºC and a resolution of 0.25ºC, to be read by the Arduino. The heat power created by the resistance, described in section 5.2, is the product of the voltage and current measured at its entrance by two different multimeters.

Following this procedure, starting from the ambient temperature, the Arduino is turned on and is controlling the power supply to give a certain value of current to the Peltier cell (e.g. 1A). In this moment, the potentiometer regulating the heat power created by the resistance is off, i.e., creating 0W. Both the hot and cold surface of the Peltier cells will adjust their values until stationary state is achieved for this situation (1A/0W). It is assumed the Peltier cell is in a stationary state when the Arduino is reading for 30 consecutive times (which is equivalent to 150 seconds) the same temperature measurements from the thermocouples. However, even though the stationary state was reached before 20 minutes, for comparative analysis the system was running for 20 minutes for a given combination of current-heat power. After 20 minutes, the heat power created by the resistance was increased to 11.4W and following this change, the Peltier cell started to transition from the stationary state achieved with the combination of 1A/0W to a stationary state achieved with the combination 1A/11.4W. After the 20 minutes where the Peltier cell transitioned between states, the heat power was changed again, this time for 22.13W and then for 30.8W, 40.67W, 47.73W and finally for 61.7W which is the maximum heat power the resistance could output.

From this test the result achieved is a certain difference $\Delta T_c$ in the temperature of the cold surface of the Peltier cell for an imposed heat power created by the resistance. This procedure was repeated for several fixed values of current equally spread within the range of working conditions of the Peltier cell (1A, 2A, 3A, 4A, 5A, 6A, 7A, 8A, and finally 8.5A) which is 0-8.5A.

### 5.4.1.2 Internal Resistance $R_m$

For the characterization of the internal resistance of the Peltier cell used, the following procedure was addressed: for a fixed current supplied to the Peltier device, the heat power created by the resistance is varied along the time. This results in a temperature difference on both surfaces of the Peltier cell. These temperature measurements are made following exactly the same procedure used to characterize the dynamic response, as described in the previous sub-section. For each 5ºC difference
in the cold surface of the Peltier cell, the voltage and current flowing at the entrance of the Peltier cell was measured with different multimeters for the voltage and current with the precision mentioned in section 5.2. In this way, one is able to obtain the relation between the cold surface of the Peltier cell and voltage across the Peltier cell as well as relation between the temperature difference between both surfaces of the Peltier cell and the voltage across the Peltier cell. It is worth noting that the current is always fixed and thus it is the voltage that changes due to the variation of the internal resistance. As in the dynamic response, the Arduino was responsible to obtaining measurements every 5 seconds and controlling the current the power supply was giving to the Peltier cell. Also, the cold surface of the Peltier cell is in contact with the resistance.

Hence, starting from ambient temperature, assume a current of 1A is applied to the Peltier cell and 0W are imposed by the resistance regulated by the potentiometer. The cold surface of the Peltier cell starts to cool. For every 5°C difference in the cold surface, the voltage across the Peltier cell is measured with a multimeter. When the cold surface has reached its minimum value, a heat power is imposed. The value of heat power imposed is not relevant for this procedure as long as it is high enough so that the temperature of the cold surface rises. For every 5°C difference, the voltage across the cell is measured. The procedure is continuously performed until the temperature of the cold surface is lower than 80°C. Afterwards the procedure is stopped, to avoid any damage to the system and to assure that one reached the highest heat power outputted by the resistance (61.7W). This procedure was repeated for several fixed values of current equally spread the Peltier cell range (1A, 2A, 3A, 4A, 5A, 6A, 7A, 8A) which is 0-8.5A. This way, it is also possible to obtain the relation between the current supplied and the internal resistance.

5.4.1.3 Seebeck Coefficient $S_m$

Regarding the characterization of the Seebeck coefficient, minor modifications were made to the setup. The procedure followed is described in the literature [26]. Hence, the Peltier cell was inverted and it is the hot surface of the Peltier cell that is in contact with the resistance instead of the cold surface which is in contact with the fan. Furthermore, in this setup no current is supplied to the Peltier cell. Starting from ambient temperature, a heat power is imposed by the resistance regulated with the potentiometer. This results in an increase of temperature of the hot surface of the Peltier cells and consequently creates a temperature difference between both surfaces of the Peltier cell. From this temperature difference, a voltage is created at the entrance of the Peltier cell due to the Seebeck coefficient. The Seebeck coefficient is the division of the voltage at the entrance of the Peltier cell and the temperature difference between its both surfaces. The heat power imposed by the resistance is not relevant as long as the temperature of the hot surface of the Peltier cell increases. This procedure is followed while the temperature of the hot surface is lower than 100°C to assure that the system is not damaged. As in the previous procedures, the voltage across the Peltier cell was measured by the multimeter Range RE-68 and the temperature measurements were acquired with the Arduino all with the same accuracy.
5.4.1.4 Thermal Conductance $K_m$

The thermal conductance was characterized using the same setup considered in the characterization of the Seebeck coefficient and this procedure is also described in the literature [26]. So, the Peltier cell is also inverted and it is the hot surface of the Peltier cell that is in contact with the resistance instead of the cold surface, which is in contact with the fan. Furthermore, in this setup no current is supplied to the Peltier cell. Starting from ambient temperature, a heat power is imposed by the resistance regulated with the potentiometer. The power imposed is well known since the potentiometer has been calibrated before. This results in an increase of the temperature of the hot surface of the Peltier cells and consequently generates a temperature difference between both surfaces of the Peltier cell. The thermal conductance $K_m$ is the division of the heat power imposed by the resistance and the temperature difference between both surfaces of the Peltier cell. This procedure is followed while the temperature of the hot surface is lower than 100ºC, also to assure that the system is not damaged. The voltage across the Peltier cell was measured by the multimeter Range RE-68 and the temperature measurements were acquired with the Arduino all with the same accuracy.

5.4.2 Proportional Integral Derivative (PID) Controller

In the present work the solution adopted was empirical and consisted of testing several solutions for each of the three terms and manually tune the different gains for each term as needed. The procedure used consisted of imposing a known heat power created by the resistance and a temperature reference and observe how rapidly the system responded to variations of heat power imposed and how the temperature measured oscillated around the reference. For each difference between the temperature read and the reference temperature the Arduino controlled the current supplied to the Peltier cell so that the error was minimized. In this case, starting from ambient temperature, a heat power of 25W was imposed and temperature readings were acquired each 5 seconds by the Arduino with the same accuracy as in the previous procedures. After 250 seconds the heat power was changed to 5W and at 500 seconds has changed once again to 25W to observe how well the controller responded to the variations in the heat power. The time of 250 seconds was chosen for each heat power imposed because it was observed that is was more than enough time for the adequately tuned controller to respond to the variation and follow the reference. The only requirement for the system was that the overshoot when variations in the heat power occurred was not higher than 1.5ºC with the exception of the initial overshooting that could not be higher than 2.5ºC. The results of this procedure will be discussed in chapter 6.

5.4.3 Final Setup

Since the transient response of the CPU is different of the resistance regulated by a potentiometer, the PID controller gains may need to be manually adjusted for this final setup. In this
context, several values were tested to infer on the best combination of each gain to adjust the controller at the final set-up. In this procedure, since a well-defined heat power could not be imposed, the CPU working load was used instead, to induce the thermal variations to the system. The procedure followed consisted of starting from 0% of the CPU load measure the temperature reading for 250 seconds. After this the CPU load was changed to 100% which is the worst case scenario. At 500 seconds the CPU load was reduced to 25% and at 750 seconds to CPU load was increased to 75%.

The temperature measurements were conducted by the Arduino each 5 seconds with the same accuracy as in the previous procedures. The CPU loads were imposed by using a code download from [59].

To study the feasibility of the system, a final test was conducted for 72 hours under 100% of the CPU load, which is the worst case scenario for the condensation system. In this test, the Arduino was measuring the temperature of each Peltier cell and the fan each 5 seconds and controlling the current supplied to the Peltier cells accordingly. One of the most important results is to measure the difference in volume of the fluid after the 72 hours, as it provides an indirect measure of the efficiency of the condensation system: low variations in the volume of fluid in the pool indicates that the vaporized liquid was successfully condensed.
Chapter 6

Results

This chapter presents the results obtained following the experimental procedures described in the previous chapter. The characterization of the Peltier cells used here is discussed in section 6.1. The performance of the implemented PID controller is analysed in section 6.2. Here, the response of the system is evaluated in by tuning the gains of the controller. At the end of this chapter, in section 3, the performance of the final set-up proposed in this work, controlled by the implemented PID controller is shown and analysed.
6.1 Characterization of the Peltier cells

In order to develop a feasible cooling system, one must characterize the Peltier cells. Besides being important, as already explained in Chapter 5, to characterize the properties of the cells under real working conditions, as they can differ significantly from those presented in the datasheet, the characterization of the cells is important to design the control system, particularly using an open-loop controller. Although a close loop (PID controller) was chosen to assure better accuracy and reliability of the system, these properties can be useful for future modifications of the control system.

Finally, there are several studies in the literature concerning the characterization of the Peltier cells, but it is recognized in many of them, that a reliable method for this characterization is very difficult to establish. Hence, despite the efforts made, quantification of the properties such as the Seebeck coefficient $S_m$ and the Thermal conductance $K_m$ are sparsely reported in practical studies, like the one proposed here and are difficult to obtain from the literature. In this context, this characterization is expected to provide useful information on how such properties can be quantified in practical studies. By doing this, one can validate the experimental procedures described in section 5.4.1.

6.1.1 Dynamic Response

Following the experimental procedure described in section 5.4.1.1 the following results were obtained for each of the fixed currents. The results depicted in this sub-section mainly allow to analyze the temporal variation of the difference $\Delta T_c$ between the initial and final temperature of the cold surface of the Peltier cell, for a combination of current/heat power imposed by the resistance $\dot{Q}_{imp}$ within the range (1-8.5A / 0-61.7W). In this procedure several considerations must be taken into account to not induce confusion. For each fixed current, the procedure starts from the ambient temperature with $\dot{Q}_{imp} = 0W$. However, when the $\dot{Q}_{imp}$ is increased, the $\Delta T_c$ obtained is cumulative and not in comparison against the ambient temperature but against the previous state as shown in Figure 6.3. In this figure one can see that for 1A of current the Peltier cell reduces the temperature of the cold surface $T_c$ if the $\dot{Q}_{imp} = 0W$. In this case the experiment starts with an initial temperature of $T_{ci} = 17.25^\circ C$ and an equilibrium is reached after 1200 seconds where the final temperature of the cold surface $T_{cf} = 5.75^\circ C$, hence the $\Delta T_c = 11.5^\circ C$ as shown in Figure 6.2. After $\dot{Q}_{imp}$ is increased to 11.4W $T_c$ starts to increase, thus the initial temperature of this new $\dot{Q}_{imp}$ is the final temperature of the previous state, hence $T_{ci} = 5.75^\circ C$ and the final temperature of the cold surface is $T_{cf} = 35.75^\circ C$ resulting in a $\Delta T_c = 30^\circ C$. 
From Figure 6.3 one can see the difference temperature \( \Delta T \) between the hot surface and cold surface of the Peltier cell. In this figure it is clear that when \( \dot{Q}_{imp} = 11.4\text{W} \), after 190 seconds \( \Delta T \) is negative. This means that the Peltier cell is unable to remove \( \dot{Q}_{imp} = 11.4\text{W} \) imposed. From equation 4.6 in chapter 4, one can see that the power removed \( \dot{Q}_c \) by the Peltier cell equals the heat power moved by the Peltier effect (first term), the second term is the Joule effect and finally the third term is the conductive heat transport.

\[
\dot{Q}_c = S_m I T_c - \frac{1}{2} I^2 R_m - K_m \Delta T
\]

This means that if \( \dot{Q}_{imp} \) is higher than \( \dot{Q}_c \), the Peltier cell is able to remove for a given current, the \( \Delta T \) between its both surfaces is negative. Hence the difference between \( \dot{Q}_{imp} \) and \( \dot{Q}_c \) is \( \dot{Q}_{cond} \), i.e., the power moved by conduction to the fan. From Figure 6.4 can be observed for \( \dot{Q}_{imp} = 11.4\text{W} \) that the temperature of the hot surface is \( T_h = 23^\circ\text{C} \) and from Figure 6.1 that \( T_c = 35.75^\circ\text{C} \), hence the \( \Delta T = -12.75^\circ\text{C} \) in Figure 6.3. Furthermore, this difference is more noticeable for higher \( \dot{Q}_{imp} \), e.g. \( \dot{Q}_{imp} = 40.67\text{W} \) where \( T_h = 29.5^\circ\text{C} \) and \( T_c = 78^\circ\text{C} \). These high negative values for \( \Delta T \) are due to the low thermal conductance of the Peltier cell which in this case acts as an insulator. This is not desired in a cooling application because it means that the Peltier cell is not allowing the power to be removed and the heated surface is not cooled.
Figure 6.2 – Dynamic response for 1A of current

Following this for $\dot{Q}_{imp} = 0\,\text{W}$, the higher $\Delta T_c$ the better because it means that starting from ambient temperature the Peltier cell is able to reduce $T_c$ more. But when $\dot{Q}_{imp}$ is increased, $\Delta T_c$ is in comparison to the final value of temperature of the previous state and not the ambient temperature and in this case the higher it is $\Delta T_c$ the more $T_c$ is increasing which is the opposite of the desired. So, for each current the higher it is $\Delta T_c$ for $\dot{Q}_{imp} = 0\,\text{W}$ the better but the higher $\Delta T_c$ is for every other $\dot{Q}_{imp}$ is worse. In this procedure it is measured the temporal variation of $\Delta T_c$ because it is $T_c$ that is relevant in a cooling application.

Figure 6.2 shows this temporal variation when the current is set to 1A and $\dot{Q}_{imp}$ is varied from 0W to 40.67W. Overall the Figure shows that the curves follow the same trend: after a steep response of system, in which $T_c$ varies significantly until $t=400$s. Afterwards it slowly increases until $t=600$s and then attains a plateau value from $t=600$ to $t=1200$s. Taking for instance the curve for $\dot{Q}_{imp} = 0\,\text{W}$, the $\Delta T_c = 11,5\,^\circ\text{C}$ after 1200s, which means that the initial temperature for the cold surface was $T_{c_i} = 17,25\,^\circ\text{C}$ and the final temperature (i.e. after the 1200s) is $T_{c_f} = 5,75\,^\circ\text{C}$ as can be seen in Figure 6.3. In this case since $\dot{Q}_{imp} = 0\,\text{W}$, all the current supplied is used to cool $T_c$. From this temperature, $\dot{Q}_{imp}$ is increased to 11.4W, starting to increase $T_c$. In this case, a $\Delta T_c = 30\,^\circ\text{C}$ was achieved resulting in the final temperature of the cold surface $T_{c_f} = 35,75\,^\circ\text{C}$ after 1200s. In this case, it means that if the comparison was made in relation to the ambient temperature, the $\Delta T_c$ would be 18.5°C instead of the 30°C that is obtained because the temperature difference is cumulative. After this, $\dot{Q}_{imp}$ is increased to
22.13W and \( T_c \) continues to increase. After reaching a new stationary state, \( \dot{Q}_{\text{imp}} \) is increased again to 30.8W and afterwards to 40.67W.

![Figure 6.3](image1.png)  
Figure 6.3 – Temperature difference between both surfaces of the Peltier cell for 1A of current

![Figure 6.4](image2.png)  
Figure 6.4 – Absolute temperature of the hot surface for 1A of current

This is true for all the cases tested, so one may argue that the Peltier cell+fan takes roughly 400s to reach 2/3 of the final \( \Delta T \) achieved in stationary state, even when large variation in \( \dot{Q}_{\text{imp}} \) occurs.

While for other currents it was possible to further increase \( \dot{Q}_{\text{imp}} \), with 1A of current \( T_c \) was higher than 80°C for \( \dot{Q}_{\text{imp}} > 40.67W \). Therefore, this was the limiting value, to assure that the system would not be damaged by overheat.

Figure 6.5 presents the results of the dynamic response of the Peltier cell for 2A of current. The same procedure was followed as with 1A of current. However, with this current it is possible to reach a higher \( \dot{Q}_{\text{imp}} \) due to lower \( T_c \) when imposing higher \( \dot{Q}_{\text{imp}} \). While comparing Figure 6.5 with Figure 6.2, it is possible to observe that for 2A the \( \Delta T_c \) achieved for \( \dot{Q}_{\text{imp}} = 0W \) is higher than the one achieved at 1A, i.e., the Peltier cell is able to cool more with a higher current. While it may not be clear, for every \( \dot{Q}_{\text{imp}} \neq 0W \), the \( \Delta T_c \) achieved are lower. This is relevant because it means that as we increase \( \dot{Q}_{\text{imp}} \), \( T_c \) increases less with a higher current supplied to the cell which is exactly what is expected in a cooling application, i.e., \( T_c \) to be the lowest possible. Again in Figure 6.5, we can observe that when large variation in \( \dot{Q}_{\text{imp}} \) occurs, the Peltier cell takes roughly 400s to reach 2/3 of the final \( \Delta T_c \) achieved in stationary state.
Figure 6.5 - Dynamic response for 2A of current

Figure 6.6 - Temperature difference between both surfaces of the Pelier cell for 3A of current

The dynamic response for 3A of current can be observed in Figure 6.7. In this figure there is noticeable difference to the previous figures. The highest $\Delta T_c$ obtained was with $\dot{Q}_{imp} = 0W$ instead of with 11.40W. This happens because with 3A of current the Peltier cell $\dot{Q}_c > 11.4W$, hence $\Delta T_c$ does not increase so much as in the previous cases. Actually, from Figure 6.6 can be observed that $\dot{Q}_{c_{\text{max}}}$ with 3A of current is close to 30.8W because it is at this $\dot{Q}_{imp}$ that $\Delta T'$ becomes negative as explained in Chapter 4. Thus, when $\dot{Q}_{c_{\text{max}}}$ surpassed, the behaviour of the system is very similar. In this case, the extra heat power $\dot{Q}_{\text{cond}}$ the Peltier cell is unable to remove is actually moved by conduction to the fan. One can wonder why the $\Delta T_c$ obtained for $\dot{Q}_{imp} = 47.77W$ is lower than with 61.70W. This happens because the increase from 40.67W to 47.77W is of 7.10W and from 47.77W to 61.70W is of 13.93W, hence the $\Delta T_c$ is also lower.

Figure 6.7 - Dynamic response for 3A of current
Figure 6.8 and Figure 6.9 present the dynamic response of the Peltier cell for 4A and 5A of current, respectively. For $\dot{Q}_{\text{imp}} = 0\text{W}$, a $\Delta T_c = 32.25^\circ\text{C}$ is achieved for 4A while for 5A a $\Delta T_c = 35^\circ\text{C}$ is achieved. These results confirm the trends discussed in the previous paragraph, i.e., the higher the current a higher $\Delta T_c$ is achieved resulting in a lower $T_c$.

Figure 6.8 - Dynamic response for 4A of current

Figure 6.9 - Dynamic response for 5A of current

Figure 6.10 and Figure 6.11 depict the dynamic response for 6A and 7A of current, respectively. In comparison with Figure 6.9, these figures show that for $\dot{Q}_{\text{imp}} = 0\text{W}$ the $\Delta T_c$ achieved is lower. This is due to Joule effect of the Peltier cell. With these currents, the Joule effect is 82W and 115W for 6A and 7A, respectively. According to the datasheet, the optimal current if 0.7 of $\text{Imax}$, which corresponds to 5.95A. After this point, the additional cooling power obtained by increased current does not compensate the additional Joule effect created by an increased current. From this analysis, it can be concluded that the one should operate between 3A-6A. Actually, as can be observed in Figure 6.12 and Figure 6.13, for 8A and 8.5A the cooling efficiency decreases considerably. This is due to a limitation of the fan. In theory, if the fan was able to remove all the heat dissipated by the Peltier cell, the $\Delta T_c$ achieved for $\dot{Q}_{\text{imp}} = 0\text{W}$ should have been higher for 8.5A. The problem is that $T_h$ increases so rapidly due to the Joule effect, as observed in Figure 6.14, that $T_c$ cannot reach lower temperatures in comparison with 5A of current. However, the highest $\Delta T$ achieved is with 8A of current as can be seen in Figure 6.15. This means that the Peltier cell behaves at it is supposed, the problem is that the fan is unable to remove the Joule effect created by the Peltier cell and $T_h$ increases. If a high performance radiator was used and could maintain the $T_h$ at lower temperatures, $T_c$ would be in fact lower. However, by using such a radiator one would be defeating the purpose of this work.
Figure 6.10 - Dynamic response for 6A of current

Figure 6.11 - Dynamic response for 7A of current

Figure 6.12 - Dynamic response for 8A of current

Figure 6.13 - Dynamic response for 8.5A of current

Figure 6.14 - Absolute temperature of the hot surface for 8.5A of current

Figure 6.15 - $\Delta T$ for $\dot{Q}_{\text{imp}} = 0W$, for each of the currents tested
To finalize, one may argue that the Peltier device takes roughly 400s to reach 2/3 of the final $\Delta T_c$ achieved in stationary state, even when large variation $Q_{imp}$ occurs as this trend is observed for every current tested. It also can be concluded that the highest $\Delta T$ achieved was with the highest current possible, which is the expected from the datasheet. However, the lowest $T_c$ was obtained with 5A. One may argue that the best range to operate the this system composed of Peltier cell+Fan is between 3-6A since for currents lower than that the Peltier cell does not have enough cooling power and for higher current the Joule effect outweighs the additional cooling power.

6.1.2 Internal Resistance $R_m$

Following the experimental procedure described in section 5.4.1.2 several interesting results were obtained. Figure 6.16 shows how the internal resistance of the Peltier cell changes with variation of the temperature difference between both surfaces of the Peltier cell for multiple currents. The values obtained were calculated using equation 4.13 in order to $R_m$ which results in:

$$R_m = \frac{V - R_m \Delta T}{I}$$

From this figure can be concluded that the internal resistance decreases with the increase of the temperature difference between the both surfaces, however this effect is much more noticeable in lower currents. Also it can be deduced that as the power drawn by the Peltier device is increased the internal resistance increases and tends to have less variation at higher currents. Damodara das et al [60] state that the electrical resistivity of bismuth telluride fins exponentially decreases with increasing temperature and is mildly temperature-dependent thermoelectric power, the latter's magnitude increasing with increasing temperature, which is qualitatively in agreement with the results presented here.

![Figure 6.16 – $R_m$ vs $\Delta T$](image-url)
6.1.3 Seebeck Coefficient $S_m$

The procedure described in section 5.4.1.3, was followed to obtain the Seebeck effect. Figure 6.17 depicts the relation obtained between the Seebeck coefficient $S_m$ and the temperature difference $\Delta T$ between the two surfaces of the Peltier cell. It is important to emphasize that this is not the Seebeck coefficient of the material, but the Seebeck coefficient of the Peltier cell as a device, taking into account its dimensions. The results were obtained by using the following formula:

$$S_m = \frac{V}{\Delta T}$$

It can be noticed that the Seebeck coefficient is roughly constant in relation to the temperature difference between the two surfaces. The average of values obtained is 0.044793 and maximum deviation obtained was of 4.3% in relation to the average. The difference observed is so small that the deviations shown can surely be attributed to the accuracy of the multimeter used and temperature readings with the Arduino. The value of Seebeck coefficient obtained is within the range of values reported in the literature, for studies performed under similar conditions. Zhang et al. [61] calculated the parameters for several Peltier cells and for a Peltier cell with the same characteristics as the one we used obtained a Seebeck coefficient of 0.048.

![Graph showing the relation between Seebeck Coefficient and $\Delta T$ between both surfaces of the Peltier cell.](image)

Figure 6.17 – Relation between Seebeck Coefficient and $\Delta T$ between both surfaces of the Peltier cell

6.1.4 Thermal Conductance $K_m$

Figure 6.18 shows the relation obtained between the Thermal conductance $K_m$ and the temperature difference $\Delta T$ between the two surfaces of the Peltier cell. These values were taken according to the procedure described in section 5.4.1.3. The following formula was used:
\[ K_m = \frac{Q_c}{\Delta T} \]

Once again, it is worth mentioning that this is not the thermal conductivity of the material, but the thermal conductance of the Peltier cell as a device, taking into account its dimensions. It can be noticed that the thermal conductance linearly increases as the temperature difference between the two surfaces increases. This trend is also in agreement with that reported by Dirmyer et al. [62]. The values obtained are also within the expected range for the thermal conductance considering the characteristics of the Peltier cell [61].

![Graph showing the relation between thermal conductance and temperature difference](image)

**Figure 6.18 - Relation between Thermal Conductance and \( \Delta T \) between both surfaces of the Peltier cell**

### 6.2 PID Controller

The characterization of the cells previously discussed is important to design the control system, particularly using an open-loop controller. Although a close-loop (PID controller) was chosen to assure better accuracy and reliability of the system, these properties previously discussed can be useful for future modifications of the control system.

Given that an analytical model of the system could not be derived, several values for each gain of the PID controller were tested within an appropriate range and the response of the system was evaluated. The final values of the gains were therefore determined from this empirical approach.

The reference used in all tests is \( T_c = 28^\circ C \). The requirements set for a good behaviour of the condensation system is that the temperature measured (which temperature?) would not go more than 1.5\(^\circ\)C above the reference for more than 10 minutes. In all following the results, the initial heat power
imposed is 25W which is changed after 250 seconds to 5W and back again to 25W after 500 seconds as can be seen in each figure.

6.2.1 Kp

The proportional term of the PID controller was tested with Kp=5.0, Kp=1.0 and Kp=0.2. The integrative term used is Ki=0.01 and the derivative term used is Kd=1.0. Figure 6.20, Figure 6.21 and Figure 6.21 show the results obtained for the proportional term Kp=5.0, Kp=0.2 and Kp=1.0, respectively. As can be seen in Figure 6.19 with Kp=5.0, whenever there is a slight variation in the heat power imposed, the overshoot of the controller is very high. When the heat power is changed at 250 seconds and 500 seconds the controller settling time is also very high. At 600 seconds one bad reading led to an increase in the current supplied which in turn led to a rise in the internal heating and controller could not follow the reference anymore. This behaviour leads to argue that a gain of 5.0 turns the controller unstable. Figure 6.20 shows the result obtained with Kp=0.2, Ki=0.01 and Kd=1.0. In this figure, it is possible to see a much more stable result and this much more noticeable when there were variations in the heat power imposed. However, when these variations occur, the overshoot is roughly 2.0ºC which is higher than the requirements. Hence, in this case one may argue that the gain is not high enough to compensate the variations imposed. A final value was tested for the proportional term which wielded the best result and was within the requirements previously set. Figure 6.21 shows the behaviour of the controller with the proportional term set for Kp=1.0. For this gain, while there is an initial overshoot of 1.25ºC, the controller is much more stable than the previous cases. After the heat power was increased at 250 seconds, there was an overshoot of 1.25ºC which was promptly corrected by the controller. At 500 seconds can be seen an overshoot of 0.75ºC with a rapid settling time of the controller. Figure 6.22 shows the comparison between the previous cases presented. While Kp=5.0 has a lower initial overshoot, it is clear that Kp=1.0 yields the best response to fluctuations in the system and a better stability.

![Figure 6.19](image1.png)  
Figure 6.19 – Kp=5.0; Ki=0.01; Kd=1.0 for \( T_{c_{\text{ref}}} = 28^\circ\text{C} \)

![Figure 6.20](image2.png)  
Figure 6.20 – Kp=0.2; Ki=0.01; Kd=1.0 for \( T_{c_{\text{ref}}} = 28^\circ\text{C} \)
6.2.2 Ki

The integrative term of the PID controller was tested with $Ki=0.05$, $Ki=0.01$ and $Ki=0.002$. The proportional term used is $Kp=1.0$ and the derivative term used is $Kd=1.0$. Figure 6.23 shows the controller with $Ki=0.05$. While for several intervals of time the controller follows the reference, the initial overshoot and settling time is high. Figure 6.24 shows the controller with the integrative term of $Ki=0.002$. In this case, the initial overshoot is still high but when the heat power is changed the overshoot is $0.75^\circ C$ which is very good taking in account that the accuracy of the MAX31855 is $0.25^\circ C$. In this case the controller oscillations are lower, the stability is better than before and the settling time is also better. Figure 6.25 shows the controller response with $Ki=0.01$. In this case, the initial overshoot is lower than the previous case but there were some oscillations after 250 seconds and the steady-state error was higher than with $Ki=0.002$. Figure 6.26 summarises the comparison between which value used for the integrative term and $Ki=0.002$ yields the best results. Although the initial overshoot is higher than with $Ki=0.01$, the controller has more stability and is less prone to oscillations. In this case, since the initial overshoot is acceptable ($1.75^\circ C$) in comparison with the required which was $1.5^\circ C$, $Ki=0.002$ was the value selected for the integrative term. The reasoning behind is that since the system supposed to be working for several days, it is preferable to have more stability in the long time than a lower initial overshoot.
The derivative term of the PID controller was tested with $K_d=5.0$, $K_d=0.2$ and $K_d=1.0$. The proportional term used is $K_p=1.0$ and the integrative term used is $K_i=0.01$. Figure 6.27 presents the controller with the derivative term of $K_d=5.0$. As can be seen, a high derivative term leads to very high oscillations. Whenever there is a slight oscillation in the temperature, for example when the temperature starts to drop, the derivative term compensates by starting to reduce the current supplied to the Peltier cell. If the derivative term is very high, this will result in a much reduced current and the Peltier cell temperature will start to rise and vice-versa. This will lead to much oscillation around the reference which is the case in Figure 6.27. In Figure 6.28, the derivative term $K_d=0.2$ is very small which will lead to a bigger initial overshoot and slow response to the derivative error. Figure 6.29 presents the controller with $K_d=1.0$. In this case, the initial overshoot is lower than with $K_d=0.2$ and the oscillations around the reference are not as noticeable as with $K_d=5.0$. This value for the derivative term yields the best result. Figure 6.30 presents the previous results side by side in which is more
noticeable the value $K_d=1.0$ yields the best result.

![Figure 6.27 - Kd=5.0; Kp=1.0; Ki=0.01 for $T_{ref} = 28^\circ C$](image1)

![Figure 6.28 - Kd=0.2; Kp=1.0; Ki=0.01 for $T_{ref} = 28^\circ C$](image2)

Based on the analysis discussed in the previous paragraphs, the gains selected which lead to the best performance of the system are $K_p=1.0$, $K_i=0.02$ and $K_d=1.0$. The final results when setting the controller with these gains is depicted in Figure 6.24. As aforementioned, there is an initial overshoot of 1.75°C that lasts for roughly 10 seconds, which is acceptable. In the long run, the highest overshoot obtained is 0.75°C which is very good considering the accuracy of the temperature readings obtained from the Arduino are 0.25°C.

![Figure 6.29 - Kd=1.0; Kp=1.0; Ki=0.01 for $T_{ref} = 28^\circ C$](image3)

![Figure 6.30 - Comparison of the derivative terms](image4)
6.3 Final Setup

Following the procedure described in section 5.4.3, several values for each gain of the PID controller were tested. The result presented in Figure 6.31 was obtained for the controller with the gains $K_p=1.0$, $K_i=0.02$ and $K_d=1.0$. The temperature reference set was $15^\circ C$. As can be seen in the figure, the CPU load was changed so that oscillations were introduced to the system. The initial overshoot is of $1.5^\circ C$ and the highest overshoot obtained when a variation occurred was $0.75^\circ C$. The fact that the best result was with the same gains that were considered the best for the previous setup leads to believe that the controller was indeed properly tuned. Also the controller appears to be more stable with the CPU than with the resistance. The reason for this is that the Peltier cell is cooling a surface that is at a temperature lower than with the resistance. The result is very satisfactory taking into account the requirements previously set.

![Figure 6.31 – PID Controller test with $T_{ref} = 15^\circ C$](image)

As described in section 5.4.3 a final test was made that lasted for 72 hours under 100% of the CPU load, which is the worst case scenario for the condensation system. The results obtained show that the direct immersion cooling is a feasible technique. The controller was able to follow the temperature reference with minimal oscillations during the 72 hours as can be seen in Figure 6.32 and the temperature of the CPU remained constant for most of the 72 hours as depicted in Figure 6.33.
Figure 6.32 – Final test of 72 hours under CPU full load

Figure 6.33 - CPU Temperature
Chapter 7

Conclusions

This chapter finalises this work, summarising conclusions and pointing out aspects to be developed in future work.
The present thesis reports the study of a controllable condensation system using Peltier cells, which was designed to be integrated in a direct immersion cooling system to cool a personal computer. In this context, several objectives were proposed to better understand the fundamental working principles of the Peltier cells and their main characteristics such as the internal physical parameters as well as its transient response. This whole analysis allowed understanding and characterizing the Peltier cells under real working conditions, which is vital to design a feasible system. In addition, the experimental characterization of the cells also allowed to propose a methodology to quantify these properties (e.g. the Seebeck coefficient and the thermal conductance) in practical studies, which is a hot topic currently debated in the literature.

Hence, in terms of the internal resistance one can conclude that the internal resistance of the Peltier cell decreases with increasing temperature of the cold surface of the Peltier cell and increases with the power supplied to the Peltier cell as described in the literature.

The dynamic response of the system (Peltier cell+cooling fan) in contact with a heated surface can be related to the variation of the temperature of the cold surface in time. In the condition in which any heat power is imposed at the cold surface, difference in $T_c$ is the result of the power removed by the cell and therefore the best performance of the system is related to an increase in this variation (the cell will act to decrease the temperature of the cold surface so the maximum $\Delta T_c$ is the ideal condition). On the contrary, as a heat power is imposed beneath the cold surface of the cell, the best performance is related to the capacity of the cell to respond in order to avoid that the temperature of the cold surface will increase. Hence in this case the desired performance leads to minimum variation of $T_c$. In this context, the thermal response of the system was evaluated in time. The results show that the response of the system is higher than expected (nearly 400s are required for the system to reach 2/3 of the temperature difference achieved in stationary state for any given current, for a given fixed current), due to the high thermal inertia associated to the entire system. However, when the condensation system was tested in the final setup, the Peltier cell response to heat flux variations was a lot faster in the order of about 20 to 30 seconds.

For the condensation to be controllable a PID controller was designed. Given that the system could not be modelled analytically the gains were determined experimentally, analysing the response of the system when the gains were varied, within determined ranges. The best results achieved were when the terms used were $K_p=1.0$, $K_i=0.002$ and $K_d=1.0$. The results were very satisfactory taking in account the requirements of the system to cool: after a temperature reference was defined, it was required than the value measured would not go above 1.5°C of the reference for more than 3 minutes. When the PID controller was tested in the setup designed for the characterization of the Peltier cells with the terms previously mentioned, the maximum overshoot obtained was 0.75°C and lasted for 15 seconds before settling back on the reference. When tested in the final setup, the maximum overshoot achieved was 0.5°C when the CPU load changed from idle to full load which is the worst case scenario. Taking into account that the accuracy of the reading temperatures was 0.25°C, the results were very satisfactory.

A final test of 72 hours with the computer under full load which is the worst case scenario was
made to evaluate the feasibility of the system. The efficiency of the condensation system can be related to the volume of liquid that remains in the pool: the efficiency of the system is the highest for the lowest variation in the volume of liquid. In an ideal situation, the level is maintained, which means that under thermodynamic equilibrium all the liquid that is vaporized could be condensed in the system developed here. Hence the volume of the fluid in the pool was measure before and after the test and only a difference in the height of fluid of $1\text{mm}$ a total of $20\text{mm}$ was registered after 72 hours of test. During this period the computer remained operational.

The fact that the control system was developed and tested under different conditions (and even different set-up configurations) allowed an empirical optimization of the controller so that the cooling system designed and controlled here is flexible and robust enough to be used in other applications. This is so, since the controller is oblivious to the heat flux created by the surface. The temperatures read by the thermocouples are integrated in the Arduino Due, which outputs a reference voltage that directly controls the current supplied by the power supply to the Peltier cell. This way, the system can be easily transferred to any other surface with little or no redesign at all. This design also allows to system to be used in more powerful CPUs with little redesigned according to the dimensions and power dissipated by the CPU. However, it is important to emphasize that the controller does not take directly into account the heat flux being created by the CPU. The variation of the temperature of the surface the Peltier cell is controlling is a direct result of heat fluxes variation. For future work, it is relevant to test the system in personal computers that dissipate more power and observe if all the fluid is properly condensed under higher heat fluxes. Depending on the TDP difference between the CPU we tested and the new CPU, a more powerful Peltier cell could be needed. This may affect the selection of the fan used and tuning of the PID controller terms. Another important test would be to increase the duration of time the CPU is continuously working, for example from 72 hours to a week.

Apart from the aforementioned adaptations of the controller which may be required when different processors are used, an important modification should be considered in a future work, in order to take a step ahead in towards obtaining a commercial system. This is related the power supply used here, which is not viable from a commercial perspective. To achieve this, several requirements must e fulfilled. First, the power supply would have to be connected to the power grid. The 220VAC from the power grid would have to be rectified and stepped down to a desired maximum current output. For example, imagine one wishes a power supply that can output 50V and 20A in continuous current. The objective would be to transform the 220VAC from the power grid and rectify it for continuous current and step down to 50V and 20A. Then one would need a way to control the current output from 0-20A accordingly to a reference voltage (0-3.3V) produced by the Arduino Due. This way, if the Arduino outputs 0V, the power supply would output 0A and if the Arduino outputted 3.3V the power supply would output 20A. This way, a remotely controllable power supply would be designed which in this case would be remotely controlled by the Arduino but could be controlled by any other device that could generate the voltage reference. The idea is to replicate the power supply used but with fewer functions as the power supply used is considerably complex.
Annex 1

Random

Brief description of annex:

Audiovisual description of the apparatus
A.1 Theory

A.1.1 Practical examples

Annex tables’ captions are inserted using the “Table_Appendix” caption type.

Annex Figures’ captions are inserted using the “Figure_Appendix” caption type.
References


